

ชื่อ _____

รหัส _____

PRINCE OF SONGKLA UNIVERSITY
FACULTY OF ENGINEERING

Midterm Examination: Semester I

Academic year: 2004

Date: 8, August 2004

Time: 9.00 – 12.00

Subject: 230 – 425 Process Dynamics and Control

Room: A 401

ทฤษฎีในการสอบ โทษขั้นต่ำ คือ ปรับตกในรายวิชาที่ทฤษฎี และพักการเรียน 1 ภาคการศึกษา

- ข้อสอบมีทั้งหมด 4 ข้อ รวม 6 หน้าไม่รวมปก และหน้าแสดงตาราง Laplace Transform and Inverse (i) ให้นักศึกษาตรวจสอบความเรียบร้อย เขียนชื่อและรหัสทุกหน้าก่อนลงมือทำข้อสอบ
- อนุญาตให้นำกระดาษจดบันทึกขนาด A4 เข้าได้ 1 แผ่นเท่านั้น
- อนุญาตให้ทำข้อสอบด้านหลังได้

ข้อ	คะแนนเต็ม
1	35
2	30
3	55
4	60
รวม	180

อาจารย์กุลชนานัฐ กปิลกาญจน์

ผู้ออกข้อสอบ

Laplace Transform Table

$f(t)$	$F(s)$
t^n	$\frac{n!}{s^{n+1}}$
e^{at}	$\frac{1}{s-a}$
$\sin kt$	$\frac{k}{s^2+k^2}$
$\cos kt$	$\frac{s}{s^2+k^2}$
$e^{at} \sin kt$	$\frac{k}{(s-a)^2+k^2}$
$e^{at} \cos kt$	$\frac{s-a}{(s-a)^2+k^2}$
$\sinh kt$	$\frac{k}{s^2-k^2}$
$\cosh kt$	$\frac{s}{s^2-k^2}$
1	$\frac{1}{s}$
$\delta(t-a)$	e^{-as}
$e^{at} f(t)$	$F(s-a)$
$f'(t)$	$sF(s) - f(0)$
$f^{(n)}(t)$	$s^n F(s) - s^{n-1} f(0) - s^{n-2} f'(0) - \dots - f^{(n-1)}(0)$
$t^n f(t)$	$(-1)^n F^{(n)}(s)$
$f(t+T) = f(t)$	$\frac{\int_0^T e^{-st} f(t) dt}{1 - e^{-sT}}$
$f(t-a)U(t-a), a \geq 0$	$e^{-as} F(s)$
$f(t)U(t-a), a \geq 0$	$e^{-as} \mathcal{L}[f(t+a)]$
$U(t-a)$	$\frac{e^{-as}}{s}$
$\int_0^t f(\tau) d\tau$	$\frac{F(s)}{s}$
$f * g(t) = \int_0^t f(\tau)g(t-\tau) d\tau$	$F(s)G(s)$

1. [35 points] Consider exothermic reaction: $A \rightarrow B$ in the continuous stirred tank reactor (CSTR) shown in Figure 1

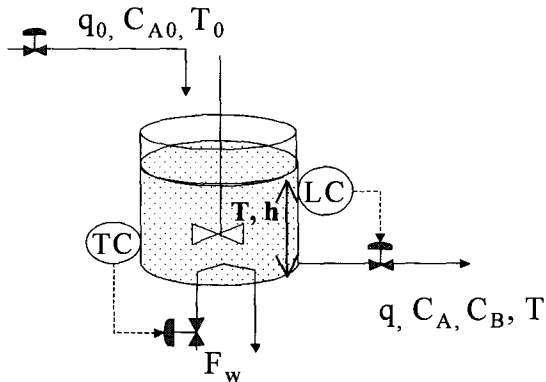


Figure 1

- q_0 = volumetric flow rate fed to the CSTR
- C_{A0} = concentration of A in the feed
- T_0 = feed temperature
- q = volumetric effluent flow
- C_A = concentration of A in the effluent
- C_B = concentration of B in the effluent
- T = effluent temperature
- F_w = cooling water flow rate
- h = reactor level

a). From the figure what are disturbance(s), controlled and manipulated variable(s)? [5]

Disturbance(s) _____

Controlled variable(s) _____

Manipulated variable(s) _____

b). If the downstream wants to get more product B and still maintain the reactor level,

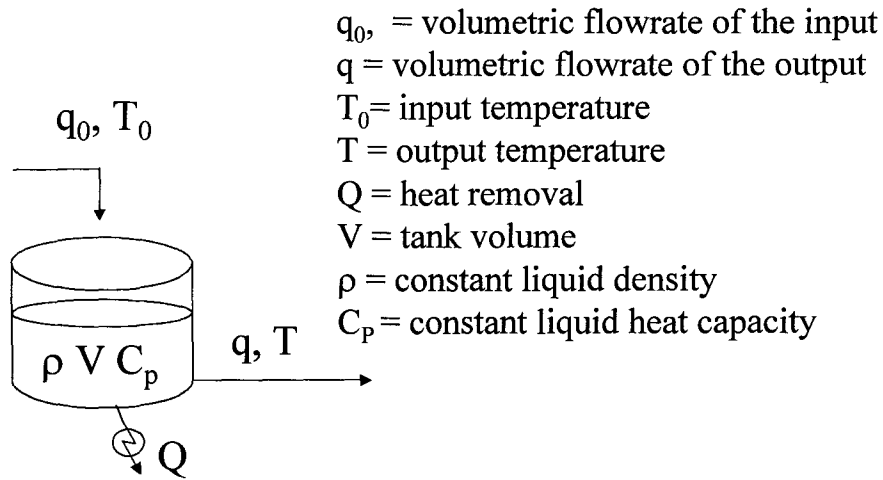
b1). Can we use the same control structure as shown in Figure 1, why? [10]

b2). The control valve for cooling water F_w should be opened or closed, why? [10]

b3). Modify figure 1 for problem b). Sketch the control structure **with feed forward and/or feed back controllers** and define variables in the structure (controlled, manipulated variables and disturbance).

[10]

2. [30 points] Consider mass and energy balances in the tank



a) Derive the mass and heat balance equations

[10]

b) From the equations, Analyze the degrees of freedom. What are the following?:

[10]

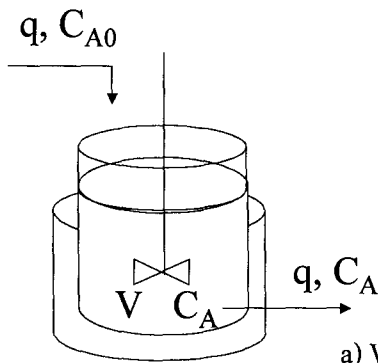
- Number of the equations $N_E =$ _____
- parameters (constants): _____
- Variables ($N_V =$ _____) : _____
- Degrees of Freedom = _____

c) From part b), is the problem can be solved? Why?

[10]

3 [55 points] Consider isothermal CSTR constant volume. IF a reaction $A \rightarrow B$ is a second order with

$$r_A = -kC_A^2. \text{ (k is constant)}$$



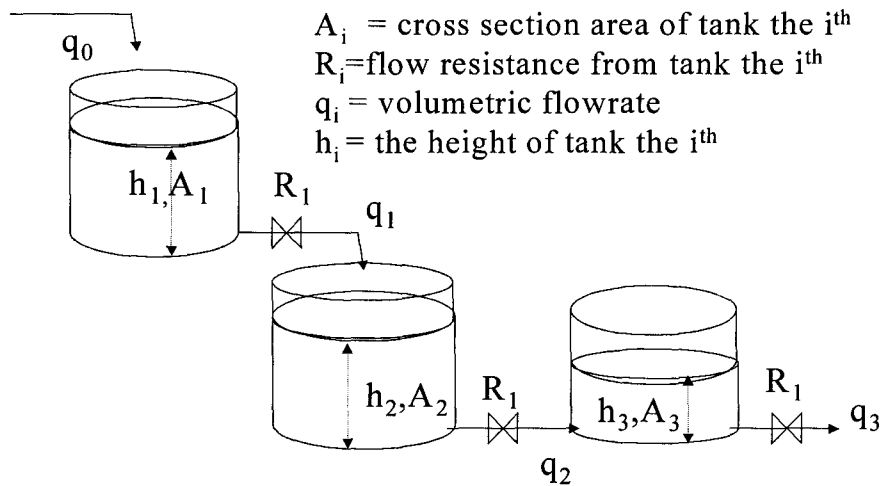
q = volumetric flow rate of the feed and effluent

C_{A0} = concentration of A in the feed

C_A = concentration of A in the reactor and the effluent

- a) Write the component A balance [10]
- b) Linearize the equation in a) if needed and find the perturbation variable [15]
- c) Use the Laplace transform to find the result (final concentration of A) when C_{A0} **increases 5%**. [25]
- d) If using Final value theory, will you get the same solution as in c) ? and Show that. [5]

- 4 [60 points] The liquid tank system is shown below:
- a) To simplify the model, what are the assumptions used in this model besides the given parameters? [5]
 - b) What is a mathematical model for material balance of this system with your assumptions in (a). [10]
 - c) Find the perturbations variables of this systems with 3 tanks [10]
 - d) Find the transfer functions for the perturbation of $G_1=Q_3(s)/Q_0(s)$ and $G_2=H_3(s)/Q_0(s)$. If the change in $Q_0(s)$ is unit step function, what are the response and the final value of $H_3(t)$ [25]
 - e) IF liquid in tank 2 and 3 are considered, what are the damping factor $G_3(s)=Q_3(s)/Q_1(s)$? [10]



Note Let $q = h/R$