

มหาวิทยาลัยสงขลานครินทร์

คณะวิศวกรรมศาสตร์

การสอบไล่ ประจำภาคการศึกษาที่ 2

ประจำปีการศึกษา 2548

วันที่ 27 กุมภาพันธ์ 2549

เวลา 09.00-12.00 น.

วิชา 211-221 Fundamentals of Electric Machines

ห้อง R200 , R201

- คำสั่ง
1. ข้อสอบมีทั้งหมด 5 ข้อ ให้ทำทุกข้อ
  2. อนุญาตให้นำเครื่องคิดเลขเข้าห้องสอบได้
  3. ห้ามนำโน้ต ตำราเรียน เข้าห้องสอบ

1. A transformer that can be consider ideal has 200 turns on its primary winding and 500 turns on its secondary winding. The primary is connected to a 220 V sinusoidal supply and the secondary supplies 10 kVA to a load
  - a. Determine the load voltage, secondary current and primary current
  - b. Find the load impedance as seen from the supply

(20 คะแนน)

2. A 2300/208 V 500 kVA 60 Hz single-phase transformer was tested by means of the open-circuit test (on the low-voltage winding) and short-circuit test (on the high-voltage winding) The test data obtained are :

Open – circuit test :  $V_{oc} = 208 \text{ V}$  ,  $I_{oc} = 52.5 \text{ A}$  ,  $P_{oc} = 3800 \text{ W}$

Short – circuit test :  $V_{sc} = 95 \text{ V}$  ,  $I_{sc} = 217.4 \text{ A}$  ,  $P_{sc} = 6200 \text{ W}$

Calculate :

- a. The voltage regulation when supplying full load at a power factor 0.866 lagging
- b. The efficiency of this transformer at full load , when the power factor is 0.866 lagging
- c. maximum efficiency when power factor is 0.866

(20 คะแนน)

3. A three – phase 125 hp 440 V 60 Hz eight pole Y connected induction motor has the following electric circuit parameters on a per phase basis referred to the stator :

$$R_s = 0.068 \Omega \quad X_s = X'_R = 0.224 \Omega$$

$$R'_R = 0.052 \Omega \quad X_m = 7.68 \Omega$$

the rotational losses are 2400 W

Calculate

- a. The starting torque
- b. The slip at which maximum torque occurs
- c. The speed at which maximum torque occurs
- d. The maximum torque

(20 คะแนน)

4. A 7.5 hp 220 V four-pole three –phase Y connected induction motor was tested and the following data were recorded :

No – load test :  $V_{NL} = 220 \text{ V}$  ,  $P_{NL} = 320 \text{ W}$  ,  $I_{NL} = 6.4 \text{ A}$

Blocked-rotor test :  $V_{BR} = 46 \text{ V}$  ,  $P_{BR} = 605 \text{ W}$  ,  $I_{BR} = 18 \text{ A}$

The dc resistance measurement on the stator winding give a 4 V drop between terminals, when dc current flows is 7.8 A

For a slip at full load is 4%

Calculate :

- a. The line current and power factor
- b. The efficiency

(20 คะแนน)

5. A  $\frac{1}{4}$  hp 120 V 60 Hz single – phase capacitor – start induction motor has a main winding impedance of  $6 \angle 45^\circ \Omega$  and an auxiliary winding impedance of  $10 \angle 15^\circ \Omega$

Calculate :

- a. The main winding current
- b. The value of capacitor which is needed in series with the starting winding to produce a  $90^\circ$  phase shift between winding current at startup

(20 คะแนน)

# Transformer

no load current  $I_0 = I_m + I_w$

$$E_p = 4.44 f N_p \phi_m$$

$$E_s = 4.44 f N_s \phi_m$$

turn ratio  $a = \frac{E_p}{E_s} = \frac{N_p}{N_s}$  ,  $\frac{I_s}{I_p} = a$

## Equivalent Circuit

$$R_{ep} = R_p + a^2 R_s \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} \text{in primary term.}$$

$$X_{ep} = X_p + a^2 X_s$$

$$R_{es} = R_s + \frac{R_p}{a^2} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} \text{in secondary term.}$$

$$X_{es} = X_s + \frac{X_p}{a^2}$$

## Open-circuit test

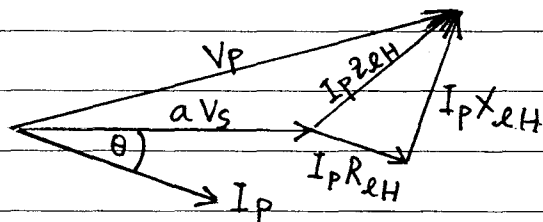
วัดวัตต์มิเตอร์  $\rightarrow$  watt-meter  $\rightarrow$  no-core losses

## Short-circuit Test

$$R_{eH} = \frac{P_{se}}{I_{se}^2}, \quad Z_{eH} = \frac{V_{se}}{I_{se}}, \quad X_{eH} = \sqrt{Z_{eH}^2 - R_{eH}^2}$$

## Voltage Regulation

$$\text{voltage regulation} = \frac{V_{\text{no-load}} - V_{\text{full-load}}}{V_{\text{full-load}}} \times 100\%$$



## Efficiency

$$\eta = \frac{\text{output power}}{\text{input power}} = \frac{\text{output power}}{\text{output power} + \text{losses}}$$

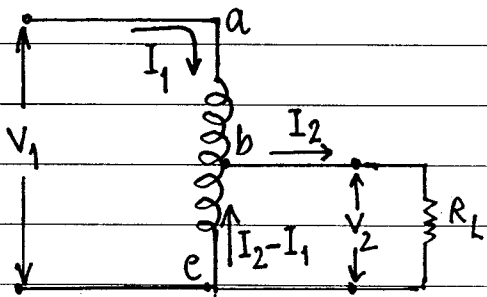
$$\eta = \frac{kVA_{out} \times PF}{kVA_{out} \times PF + \text{copper losses} + \text{core loss}}$$

The efficiency is maximum when the copper losses equal the core losses

### All-day Energy Efficiency

$$\eta_e = \frac{\text{energy output over 24 hours}}{\text{energy input over 24 hours}}$$

### Autotransformer



$P_e = V_2 I_1 =$  Conducted power to load through ab

$P_{tr} = V_2 (I_2 - I_1) =$  transformed power to load through bc

### Induction Motor

synchronous speed  $n_s = \frac{120f}{P}$  r/min

slip  $S = \frac{n_s - n_r}{n_s} \times 100\%$

rotor speed  $n_r = (1 - S) \times n_s$  r/min

rotor power input (RPI) = rotor copper loss (RCL) + rotor power developed (RPD)

$RPI \text{ (per phase)} = I_R^2 \frac{R_R}{S}$

$RCL = I_R^2 R_R$

$RPD = I_R^2 R_R \frac{1 - S}{S} = RPI (1 - S)$

developed torque  $T_d = \frac{RPD}{\omega_r}$  N-m.

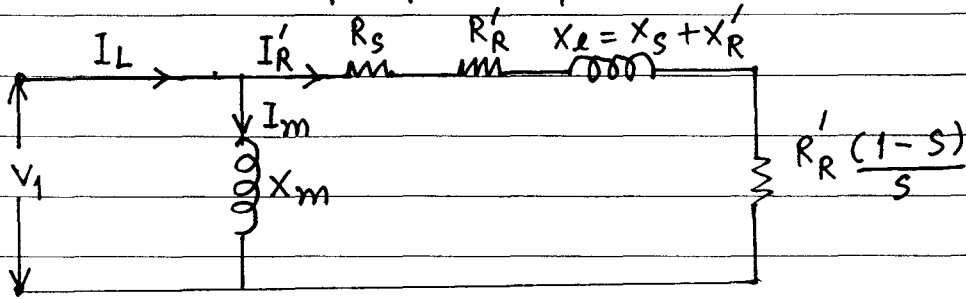
$\omega_r = \frac{2\pi n_r}{60}$  rad/s

shaft torque  $T = \frac{RPD - P_{rot}}{\omega_r}$

$$P_{out} = RPD - P_{rot}$$

$P_{rot}$  = rotational loss = friction, windage and core losses

Equivalent circuit per phase of Induction motor



เมื่อ stator winding หน่วงแบบ Y และใช้ค่าสมมติว่าพิกัด voltage ของมอเตอร์  
คือ 220 V. ,  $V_1$  คือ phase voltage =  $\frac{220}{\sqrt{3}}$  V.

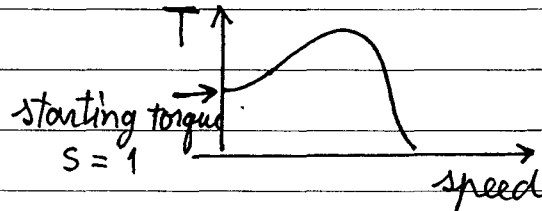
$$I'_R = \frac{V_1}{(R_s + \frac{R'_R}{s}) + j(X_s + X'_R)}$$

$$I_m = \frac{V_1}{jX_m}, \quad I_L = I_m + I'_R$$

Starting Torque

$$T_{st} = \frac{RPI_{st}}{\omega_s}$$

$$\text{เมื่อ } \omega_s = \frac{2\pi N_s}{60}$$



Maximum Torque

$$s_{mt} = \frac{R'_R}{\sqrt{R_s^2 + (X_s + X'_R)^2}}$$

$$T_{mt} = \frac{RPD_{mt} - P_{rot}}{\omega_{rmt}}$$

No-load test

$$P_{NL} = P_c + P_{fr+w} + 3 I_{NL}^2 R_s$$

$$P_{rot} = P_{NL} - 3 I_{NL}^2 R_s$$

$$\therefore P_{rot} = P_c + P_{fr+w} = \text{friction} + \text{windage} + \text{core losses}$$

$$X_m = \frac{V_{NL}}{\sqrt{3} I_{NL}}$$

Blocked Rotor Test

$$Z_e = \frac{V_{BR}}{\sqrt{3} I_{BR}} = \sqrt{(R_s + R'_r)^2 + j(X_s + X'_r)^2}$$

$$R_e = \frac{P_{BR}}{3 I_{BR}^2} = R_s + R'_r$$

$$X_e = \sqrt{Z_e^2 - R_e^2} = X_s + X'_r$$

$$X_s = X'_r = 0.5 X_e$$