

**PRINCE OF SONGKLA UNIVERSITY  
FACULTY OF ENGINEERING**

Midterm Examination: Semester I

Academic year: 2006

Date: 6 August 2006

Time: 9.00-12.00

Subject: 230 – 425 Process Dynamics and Control

Room: A401

ทฤษฎีในการสอบ โทษขั้นต่ำ คือ ปรับตกในรายวิชาที่ทฤษฎี และพักการเรียน 1 ภาคการศึกษา

- **Only hand written note in 1 A4 and a dictionary are allowed.**
- There are 8 pages of the exam.
- Write your name or at least your code on each page.
- If need to write the answers on the back of each page, please identify the problem number.
- Write explanations clearly and concisely will be your advantage.
- Calculator, Dictionary and hand-written in 1 A4 are allowed.

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Problem Number	Score	
1	20	
2	15	
3	35	
4	50	
5	45	
6	15	
Total	180	

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**Laplace transform**

<b>F(s)</b>	<b>f(t), t &gt; 0</b>
$Y(s) = \int_0^{\infty} \exp(-st)y(t)dt$	$y(t)$
$Y(s)$	$y(t) = \frac{1}{j2\pi} \int_{c-j\infty}^{c+j\infty} \exp(st)Y(s) ds$
$s^n Y(s) - s^{n-1}[y(0)]$ $- s^{n-2}[y'(0)] - \dots - s[y^{(n-2)}(0)]$ $- [y^{(n-1)}(0)]$	$y^{(n)}(t)$
$F(s)/s$	$\int_0^t Y(\tau) d\tau$
$F(s)G(s)$	$\int_0^t f(t-\tau)g(\tau) d\tau$
$\frac{1}{\alpha} F\left(\frac{s}{\alpha}\right)$	$f(\alpha t)$
$F(s-\alpha)$	$\exp(\alpha t)f(t)$
1	$\delta(t)$
$\exp(-\alpha s), \alpha \geq 0$	$\delta(t-\alpha)$
1/s	$u(t)$
1/s exp(-\alpha s)	$u(t-\alpha)$
1/s <sup>2</sup>	t
s <sup>-n</sup> n=1, 2, 3,...	t <sup>n-1</sup> / (n-1)!
n! / s <sup>n+1</sup> n=1, 2, 3,...	t <sup>n</sup>
$\frac{1}{(s+\alpha)^n}, n=1, 2, 3, \dots$	$\left[ \frac{t^{n-1}}{(n-1)!} \right] \exp(-\alpha t)$
$\frac{\alpha}{s^2 + \alpha^2}$	$\sin(\alpha t)$
$\frac{s}{s^2 + \alpha^2}$	$\cos(\alpha t)$
$\frac{1}{s^2 - \alpha^2}$	$\frac{1}{\alpha} \sinh(\alpha t)$
$\frac{s}{s^2 - \alpha^2}$	$\cosh(\alpha t)$

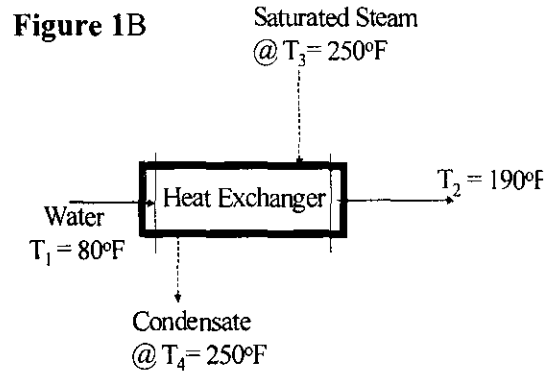
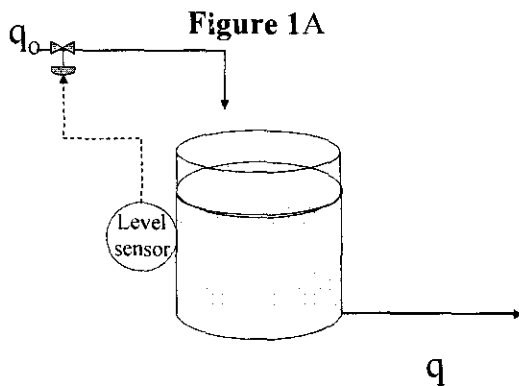
1 (20 points)

1.1 (10 points) From Figure 1A, please answer the questions

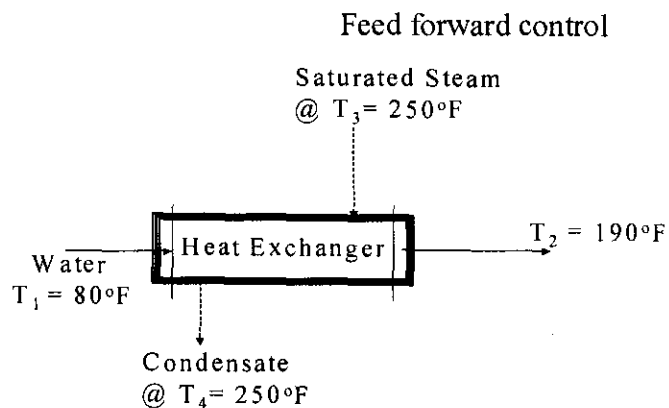
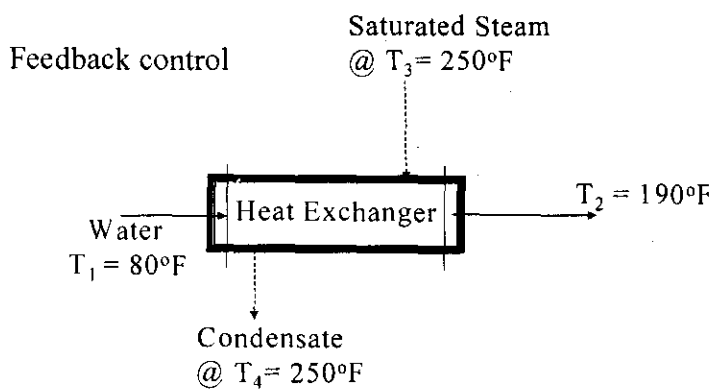
a. Controlled variable is \_\_\_\_\_ b. Disturbance is \_\_\_\_\_

c. Manipulated variable is \_\_\_\_\_

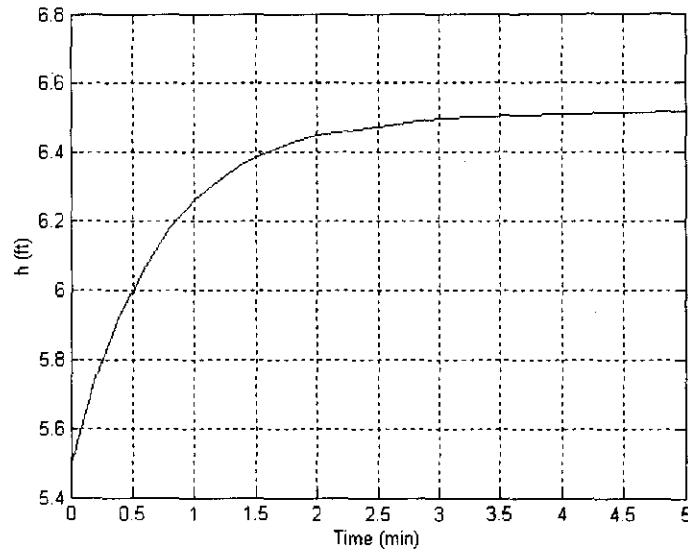
d. Does the figure show feedback control or feed forward control? Give the reasons that make you select your answer. \_\_\_\_\_



1.2 (10 points) From Figure 1B, consider the temperature  $T_2 = 190^\circ\text{F}$  is our basic control objective. Construct feedback and feed forward control configurations that will satisfy the control objective



2. (15 points) A single-tank process has been operating for a long period of time with the inlet flow rate  $q_i = 30.4 \text{ ft}^3/\text{min}$ . After the operator increases the flow rate suddenly by 10%, the liquid level in the tanks changes as shown in Figure 2



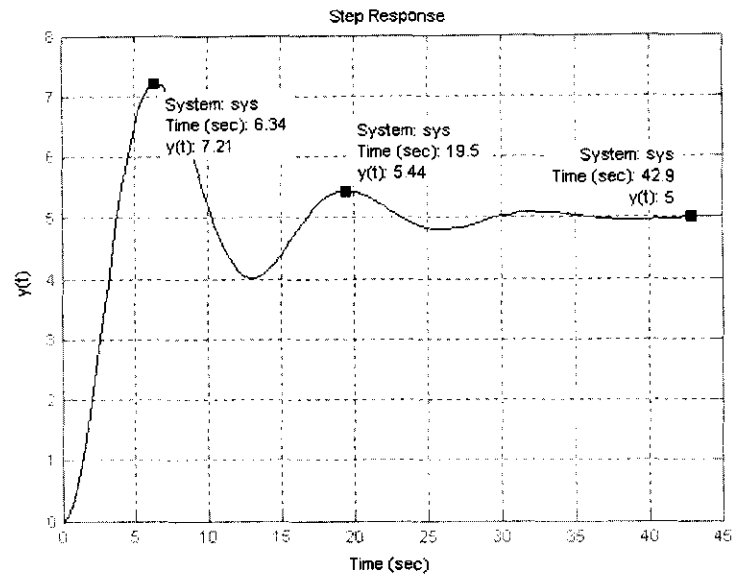
**Figure 2** Display liquid level in a single-tank process

2.1 The order of the process is \_\_\_\_\_

2.2 Does the process has transportation lag? If it has, what is the value of the lag?

2.3 Show the transfer function of the process

3. (35 points)



**Figure 3** step response of the process

If step input is 2, determine the following variables:

3.1 Process gain \_\_\_\_\_ 3.2 Overshoot \_\_\_\_\_

3.3 Period \_\_\_\_\_

3.4 Damping factor \_\_\_\_\_

3.5 Process time constant \_\_\_\_\_

3.6 Process transfer function \_\_\_\_\_

4. (50 points) Two isothermal CSTRs are connected by a long pipe that acts as pure deadtime of  $D$  minutes at the steady-state flow rate. Assume constant throughput and holdups and first-order irreversible reaction  $A \rightarrow B$  with reaction rate constant  $k$  in each tank.
- 4.1. Derive the transfer function relating the feed concentration to the first tank,  $C_{A0}$ , and the concentration of A in the stream leaving the second tank,  $C_{A2}$ .
- 4.2 Find  $C_{A2}(0)$ ,  $C_{A2}(t=\infty)$  and  $C_{A2}(t)$  for a unit step disturbance in  $C_{A0}$

5. (50 points) Figure 4 shows 2-tank process with constant liquid density. If  $F_0$ ,  $F_1$  and  $F_2$  are volumetric flow rates,  $A_1$ ,  $V_1$ ,  $A_2$  and  $V_2$  are cross section areas and liquid volumes of tank 1 and tank 2, respectively. If the relation of flow rate  $F_1$  and liquid level of tank 1 ( $h_1$ ) is  $F_1 = h_1 / R_1$  and for tank 2 is  $F_2 = \sqrt{h_2} / R_2$ .

5.1 Determine  $\frac{H_2(s)}{F_0(s)}$

5.2 Show the damping factor of the transfer function from 5.1.

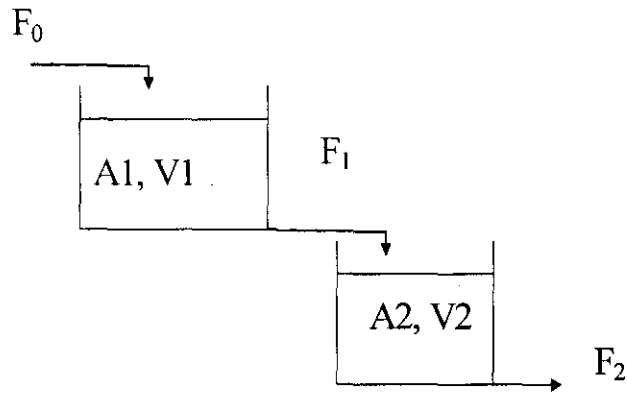


Figure 4

6. (15 points) Show transfer function of  $\frac{x_1(s)}{x_0(s)}$  for the process in figure 5

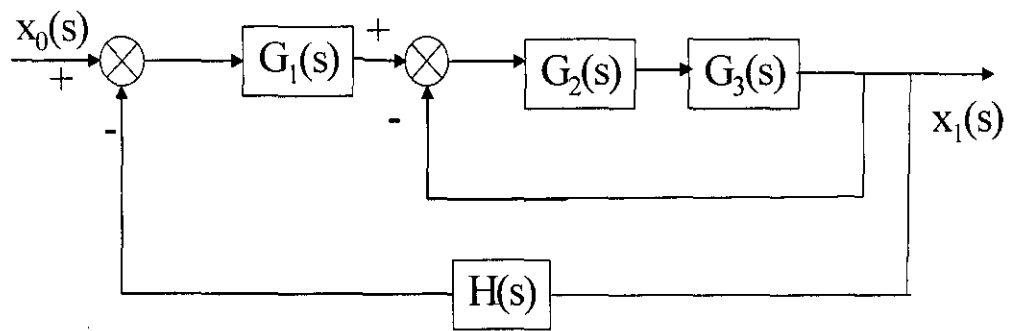


Figure 5