

มหาวิทยาลัยสงขลานครินทร์  
คณะวิศวกรรมศาสตร์

สอบปลายภาค ประจำปีภาคการศึกษา 1

วันที่ 10 ตุลาคม 2550

วิชา CE 220-302,221-302: Structural Analysis 1

ปีการศึกษา 2550

เวลา 09.00 – 12.00.

ห้องสอบ R 200

ชื่อ-สกุล

รหัส

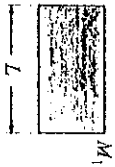
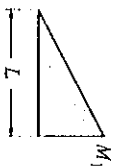
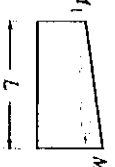

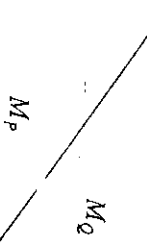
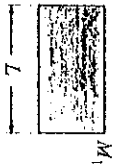
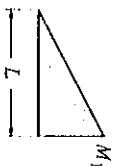
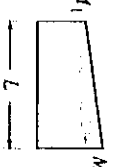



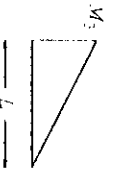

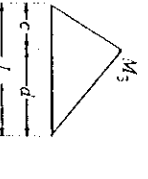
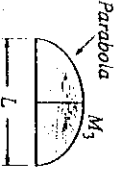
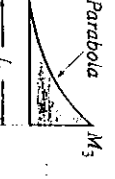
คำชี้แจง

1. ข้อสอบทั้งหมดมี 6 ข้อ คะแนนรวม 100 คะแนน ดังแสดงในตารางข้างล่าง
2. ข้อสอบมีทั้งหมด 14 แผ่น (รวมปก) ผู้สอบต้องตรวจสอบว่ามีครบทุกหน้าหรือไม่ (ก่อนลงมือทำ)
3. ให้ทำหมดทุกข้อลงในตัวข้อสอบถ้าไม่พอให้ใช้หน้าหลังได้
4. อนุญาตให้ใช้เครื่องคิดเลขได้ทุกชนิด
5. ห้ามหยิบ หรือยืมสิ่งของใดๆ ของผู้อื่นในห้องสอบ ทุกจริตติด E
6. **GOOD LUCK**

ตารางคะแนน

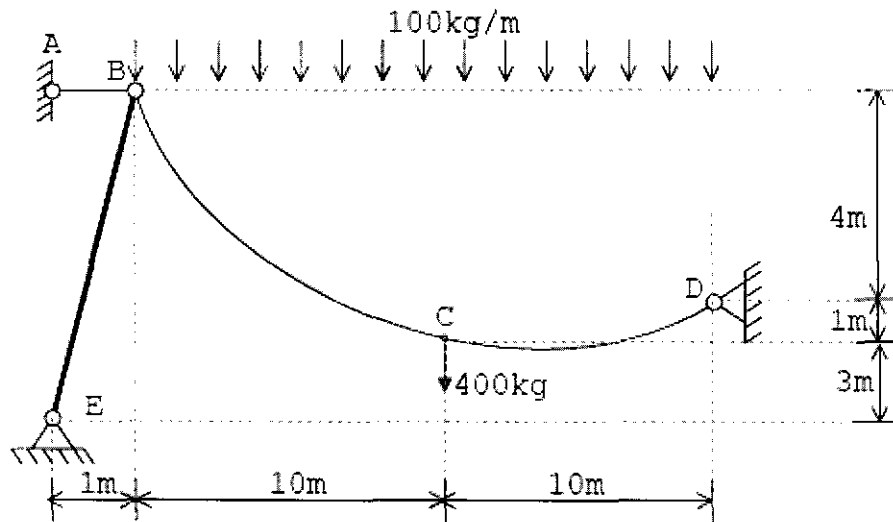
ข้อที่	คะแนนเต็ม	ได้
1	15	
2	10	
3	15	
4	20	
5	20	
6	20	
รวม	100	

Table 4: Values of Product Integrals  $\int_{x=0}^{x=L} M_Q M_P dx$

				
				
	$M_1 M_3 L$	$\frac{1}{2} M_1 M_3 L$	$\frac{1}{2} (M_1 + M_2) M_3 L$	$\frac{1}{2} M_1 M_3 L$
	$\frac{1}{2} M_1 M_3 L$	$\frac{1}{3} M_1 M_3 L$	$\frac{1}{6} (M_1 + 2M_2) M_3 L$	$\frac{1}{6} M_1 M_3 (L + a)$
	$\frac{1}{2} M_1 M_3 L$	$\frac{1}{6} M_1 M_3 L$	$\frac{1}{6} (2M_1 + 2M_2) M_3 L$	$\frac{1}{6} M_1 M_3 (L + b)$
	$\frac{1}{2} M_1 (M_3 + M_2) L$	$\frac{1}{6} M_1 (M_3 + 2M_2) L$	$\frac{1}{6} M_1 (2M_2 + M_1) L$ $-\frac{1}{6} M_2 (M_3 + 2M_1) L$	$\frac{1}{6} M_1 M_3 (L + b)$ $-\frac{1}{6} M_2 M_3 (L + a)$
	$\frac{1}{2} M_1 M_3 L$	$\frac{1}{6} M_1 M_3 (L - c)$	$\frac{1}{6} M_1 M_3 (L + d)$ $-\frac{1}{6} M_2 M_3 (L + c)$	for $c \leq a$ : $\left( \frac{1}{3} - \frac{(a-c)^2}{6ad} \right) M_1 M_3 L$
	$\frac{2}{3} M_1 M_3 L$	$\frac{1}{3} M_1 M_3 L$	$\frac{1}{3} (M_1 + M_2) M_3 L$	$\frac{1}{3} M_1 M_3 \left( L + \frac{ab}{L} \right)$
	$\frac{1}{3} M_1 M_3 L$	$\frac{1}{4} M_1 M_3 L$	$\frac{1}{12} (M_1 + 3M_2) M_3 L$	$\frac{1}{12} M_1 M_3 \left( 3a + \frac{a^2}{L} \right)$

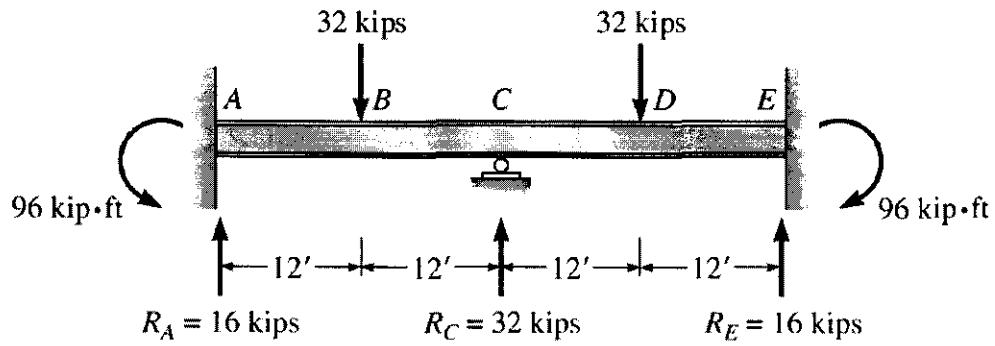
**Problem 1 (15 Points)**

For the cable structure shown below, compute the maximum and minimum tension in the cable BD, the tension in cable AB, the support reactions at D and the resultant force in member BE.



**Problem 2 (10 Points)**

Using the moment-area method, compute the slope and deflection under 32 kips load at B. Reactions are given.  $I = 510 \text{ in}^4$  and  $E = 29,000 \text{ kips/in}^2$ . Sketch the deflected shape.



**Problem 3 (15 Points)**

From the beam below, Use the virtual work method to determine:

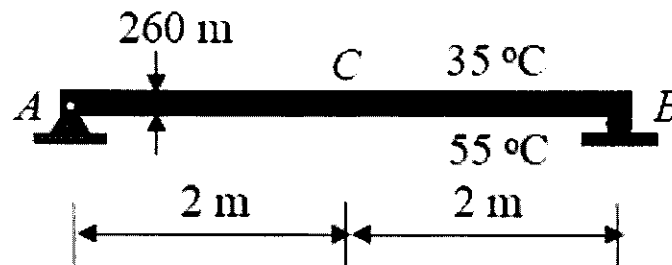
(a) If  $P = 50 \text{ kN}$  is applied at the mid-span  $C$ , what would be the displacement at point  $C$ . Due to shear and bending moment.

(b) If the temperature at the top surface of the beam is  $35 \text{ }^\circ\text{C}$ , the temperature at the bottom surface is  $55 \text{ }^\circ\text{C}$  and the room temperature is  $20 \text{ }^\circ\text{C}$ .

What would be the vertical deflection of the beam at its midpoint  $C$  and the horizontal displacement of the beam at support  $B$ .

(c) If (a) and (b) are both accounted, what would be the vertical displacement of the beam at its midpoint  $C$ .

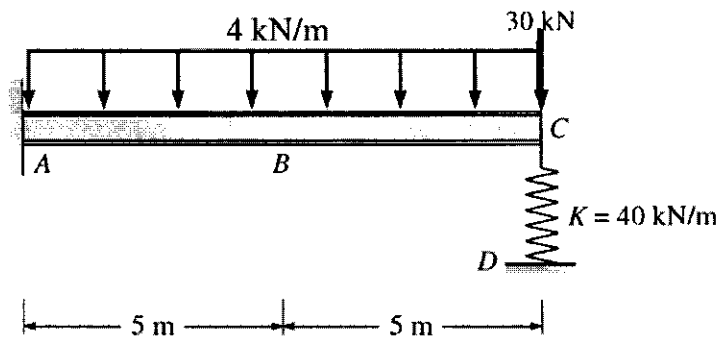
Take  $\alpha = 12(10^{-6})/^\circ\text{C}$ .  $E = 200 \text{ GPa}$ ,  $G = 80 \text{ GPa}$ ,  $I = 200(10^6) \text{ mm}^4$  and  $A = 35(10^3) \text{ mm}^2$ . The cross-section area is rectangular ( $K = 1.2$ ).



**Problem 4 (20 Points)**

For the beam shown below, in addition to the applied load, the support at D settles by 0.2 m.  $EI$  is constant for the beam.  $E = 200\text{GPa}$ ,  $I = 160(10^6)\text{mm}^4$ .

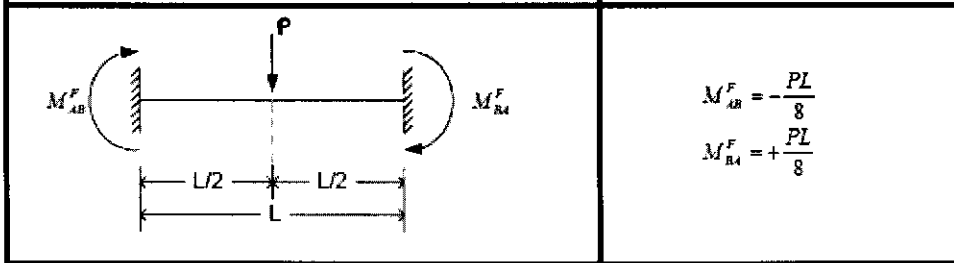
- (a) Compute the reactions at A and C and also vertical displacement at C by the virtual work method.
- (b) Draw the shear and moment curves.



**Problem 5 (20 Points)**

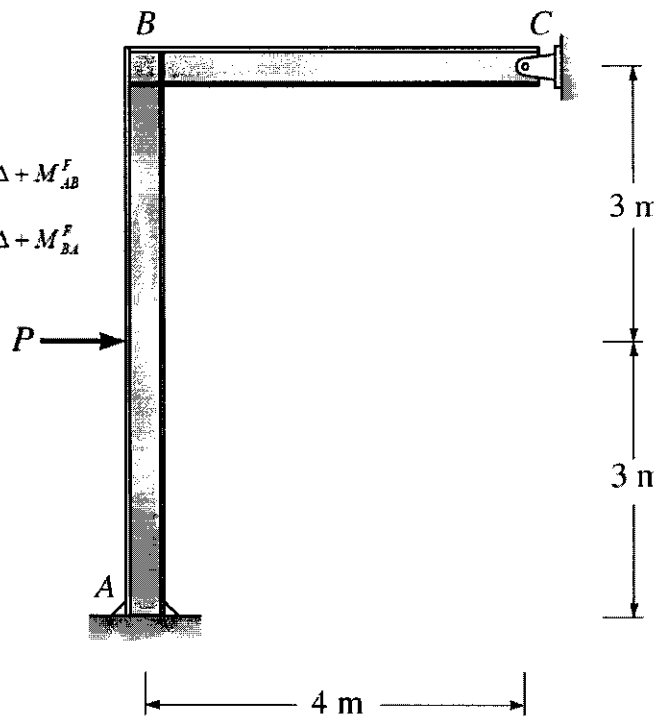
Analyze the structure in the following figure by the slope-deflection method. In addition to the applied load, support *A* rotates counterclockwise by 0.015 rad. Also  $P = 100 \text{ kN}$ ,  $EI$  is constant for all members,  $E = 200 \text{ GPa}$ ,  $I = 25 \times 10^6 \text{ mm}^4$ .

Hint:



$$M_{AB} = \frac{4EI}{L} \theta_A + \frac{2EI}{L} \theta_B - \frac{6EI}{L^2} \Delta + M_{AB}^F$$

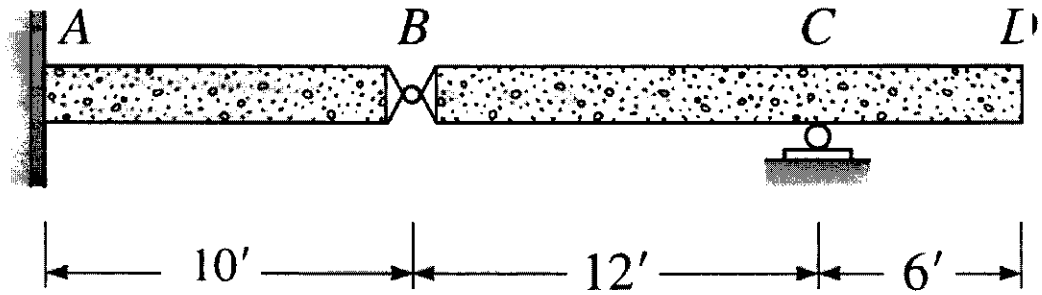
$$M_{BA} = \frac{2EI}{L} \theta_A + \frac{4EI}{L} \theta_B - \frac{6EI}{L^2} \Delta + M_{BA}^F$$



**Problem 6 (20 Points)**

Using the Muller-Breslau principle,

- a) Draw the influence lines for the moment and vertical reaction at  $A$ , the moment at  $C$  and the shear at the left of support  $C$ .





- b) For the beam shown below, draw the influence lines for the reactions at  $A$ ,  $B$  and  $F$ , the end moment at  $F$ , shears to the left and right of support  $B$  and shear at  $E$ .

