

**Faculty of Engineering
Prince of Songkla University**

Final Examination

October 8th, 2007

221 – 361 Surveying II

1st Semester 2007

Room A401

Time: 9:00 - 12:00 (3 hours)

Instructions

1. There are 5 problems in this exam. (100 points)
2. Attempt all problems.
3. Books and lecture notes are not allowed.
4. Students can bring in calculators and dictionaries.
5. Students can use pencils in the answer books.

นาย รจ ศุภวิไล ผู้ออกข้อสอบ

- 1) Explain the effects of parallax and refraction on astronomical observation. Also sketch the diagram that clearly shows the relations among parallax, refraction, altitude of a celestial body and the position of the observer. (10 points)
- 2) On October 11th, the observed altitude of the sun at the station A is $31^{\circ} 20' 35''$ at $14^{\text{h}} 41^{\text{m}} 35^{\text{s}}$ local time. The latitude of A is $37^{\circ} 52' 20''$ N and the longitude of A is 120° W. The temperature during the observation is 75°F and the barometric pressure is $29.3''$ Hg. The mean horizontal angle (measured clockwise) from the reference station B to the sun is $60^{\circ} 01' 57''$. Compute the azimuth of the sun as well as the azimuth of the reference line AB. (25 points) Hint: GMT = Local time + 8h
- 3) Prepare the table required for staking out at every 100 ft. full station of a horizontal curve by deflection angle method. Given the degree of the curve $D_a = 12^{\circ}$ according to the arc definition (Arc basis). the deflection angle $\theta = 104^{\circ} 36'$ and the stationing at PI = $96+03.900$ ft. Also calculate the stationings of PC and PT. (Using feet as a unit of measurement) (25 points)
- 4) An entering grade of -2.75% meets a departing grade of $+1.25\%$ at station $18+050.00$ km. The two grades intersect at an elevation of 123.190 m. above mean sea level. If these two grades are connected by a 300-m equal-tangent parabolic curve, computing the elevation of points BVC, EVC and all full stations POC for every 20m . Also determine the location and elevation of the lowest point on the curve. (25 points)
- 5) From the astronomical triangle PZS where P is the north celestial pole, Z is the observer's zenith and S is the celestial body (the star). Using the principle of spherical trigonometry show that.

$$\cos Z = (\sin \delta / \cos h \cos \Phi) - \tan h \tan \Phi$$

Where

- δ = declination of the celestial body
 h = altitude of the celestial body
 Φ = latitude of the observer
 Z = azimuth of the celestial body

(15 points)

TABLE 1
SOLAR EPHEMERIS OCTOBER 1984
For 0h Universal Time or Greenwich Civil Time

| Day of Month & Week | The Sun's Apparent Declination | Diff in Declin for 1 hour | Equation of Time | | | GHA of Polaris |
|---------------------|--------------------------------|---------------------------|-------------------------|-------------------|----------------|----------------|
| | | | True Sol. Time = (L.T.) | Differ for 1 hour | GHA of Polaris | |
| 1 M | S03 10.3 | 0.97 | +10 16.3 | 0.80 | 335 | 41.2 |
| 2 TU | S03 33.5 | 0.97 | +10 35.5 | 0.79 | 336 | 40.1 |
| 3 W | S03 56.7 | 0.97 | +10 54.4 | 0.78 | 337 | 39.1 |
| 4 TH | S04 19.9 | 0.96 | +11 13.0 | 0.76 | 338 | 38.0 |
| 5 FR | S04 43.0 | 0.96 | +11 31.3 | 0.75 | 339 | 37.0 |
| 6 SA | S05 06.1 | 0.96 | +11 49.2 | 0.73 | 340 | 36.0 |
| 7 SU | S05 29.1 | 0.96 | +12 06.7 | 0.71 | 341 | 35.0 |
| 8 M | S05 52.0 | 0.95 | +12 23.9 | 0.70 | 342 | 34.0 |
| 9 TU | S06 14.9 | 0.95 | +12 40.6 | 0.68 | 343 | 33.0 |
| 10 W | S06 37.6 | 0.94 | +12 56.9 | 0.66 | 344 | 32.0 |
| 11 TH | S07 00.3 | 0.94 | +13 12.7 | 0.64 | 345 | 31.0 |
| 12 FR | S07 22.9 | 0.94 | +13 28.0 | 0.62 | 346 | 29.9 |
| 13 SA | S07 45.4 | 0.93 | +13 42.8 | 0.59 | 347 | 28.9 |
| 14 SU | S08 07.8 | 0.93 | +13 57.1 | 0.57 | 348 | 27.8 |
| 15 M | S08 30.0 | 0.92 | +14 10.8 | 0.55 | 349 | 26.8 |
| 16 TU | S08 52.2 | 0.92 | +14 24.0 | 0.52 | 350 | 25.7 |
| 17 W | S09 14.2 | 0.91 | +14 36.5 | 0.50 | 351 | 24.7 |
| 18 TH | S09 36.1 | 0.91 | +14 48.5 | 0.47 | 352 | 23.7 |
| 19 FR | S09 57.8 | 0.90 | +14 59.8 | 0.45 | 353 | 22.7 |
| 20 SA | S10 19.4 | 0.89 | +15 10.5 | 0.42 | 354 | 21.8 |
| 21 SU | S10 40.9 | 0.89 | +15 20.5 | 0.39 | 355 | 20.9 |
| 22 M | S11 02.2 | 0.88 | +15 29.8 | 0.36 | 356 | 20.0 |
| 23 TU | S11 23.4 | 0.87 | +15 38.5 | 0.33 | 357 | 19.1 |
| 24 W | S11 44.3 | 0.87 | +15 46.5 | 0.30 | 358 | 18.1 |
| 25 TH | S12 05.1 | 0.86 | +15 53.7 | 0.27 | 359 | 17.2 |
| 26 FR | S12 25.7 | 0.85 | +16 00.2 | 0.24 | 000 | 16.2 |
| 27 SA | S12 46.1 | 0.84 | +16 06.1 | 0.21 | 001 | 15.2 |
| 28 SU | S13 06.4 | 0.83 | +16 11.1 | 0.18 | 002 | 14.2 |
| 29 M | S13 26.4 | 0.82 | +16 15.5 | 0.15 | 003 | 13.2 |
| 30 TU | S13 46.2 | 0.82 | +16 19.1 | 0.12 | 004 | 12.3 |
| 31 W | S14 05.8 | 0.81 | +16 21.9 | 0.09 | 005 | 11.4 |
| 32 TH | S14 25.1 | | +16 23.9 | | 006 | 10.5 |

Hourly differences in declination and equation of time are for the 24 hours following 0-hours of date in left column.

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TABLE 2

REFRACTION AND SUN'S PARALLAX

(To be applied to observed altitudes. See page 16)
Bar. = 29.6 in. Temp. = 50°F

| Measured Altitude | Refraction | Sun's Par. | Measured Altitude | Refraction | Sun's Par. |
|-------------------|------------|------------|-------------------|------------|------------|
| 7 30 | 6.88 | 0.15 | 17 30 | 3.02 | 0.14 |
| 7 40 | 6.75 | 0.15 | 18 00 | 2.93 | 0.14 |
| 7 50 | 6.62 | 0.15 | 18 30 | 2.85 | 0.14 |
| 8 00 | 6.50 | 0.15 | 19 00 | 2.77 | 0.14 |
| 8 10 | 6.37 | 0.15 | 19 30 | 2.70 | 0.14 |
| 8 20 | 6.25 | 0.15 | 20 00 | 2.62 | 0.14 |
| 8 30 | 6.13 | 0.15 | 21 00 | 2.48 | 0.14 |
| 8 40 | 6.02 | 0.15 | 22 00 | 2.36 | 0.14 |
| 8 50 | 5.92 | 0.15 | 23 00 | 2.25 | 0.14 |
| 9 00 | 5.82 | 0.15 | 24 00 | 2.15 | 0.14 |
| 9 10 | 5.72 | 0.15 | 25 00 | 2.05 | 0.14 |
| 9 20 | 5.63 | 0.15 | 26 00 | 1.96 | 0.13 |
| 9 30 | 5.53 | 0.15 | 27 00 | 1.88 | 0.13 |
| 9 40 | 5.43 | 0.15 | 28 00 | 1.80 | 0.13 |
| 9 50 | 5.34 | 0.15 | 29 00 | 1.73 | 0.13 |
| 10 00 | 5.26 | 0.15 | 30 00 | 1.66 | 0.13 |
| 10 20 | 5.10 | 0.15 | 31 00 | 1.53 | 0.13 |
| 10 40 | 4.95 | 0.14 | 34 00 | 1.42 | 0.12 |
| 11 00 | 4.81 | 0.14 | 36 00 | 1.32 | 0.12 |
| 11 20 | 4.67 | 0.14 | 38 00 | 1.23 | 0.12 |
| 11 40 | 4.54 | 0.14 | 40 00 | 1.15 | 0.11 |
| 12 00 | 4.42 | 0.14 | 42 00 | 1.07 | 0.11 |
| 12 30 | 4.25 | 0.14 | 44 00 | 1.00 | 0.11 |
| 13 00 | 4.09 | 0.14 | 46 00 | 0.93 | 0.10 |
| 13 30 | 3.93 | 0.14 | 48 00 | 0.86 | 0.10 |
| 14 00 | 3.78 | 0.14 | 50 00 | 0.80 | 0.09 |
| 14 30 | 3.65 | 0.14 | 55 00 | 0.67 | 0.08 |
| 15 00 | 3.53 | 0.14 | 60 00 | 0.55 | 0.07 |
| 15 30 | 3.42 | 0.14 | 65 00 | 0.45 | 0.06 |
| 16 00 | 3.32 | 0.14 | 70 00 | 0.35 | 0.05 |
| 16 30 | 3.22 | 0.14 | 80 00 | 0.17 | 0.03 |
| 17 00 | 3.12 | 0.14 | 90 00 | 0.00 | 0.00 |

The refraction values in Table 2 are corrected by multiplying them by the multipliers in Table 2a when the barometric pressure and the temperature differ from those on which Table 2 is based, i.e. 29.6 inches and 50°F.

If the barometric pressure is not known, it may be estimated from the elevation of the locality in accordance with the values given in Table 2a. Otherwise the elevations are disregarded.

TABLE 1
SOLAR EPHEMERIS NOVEMBER 1984
For 0h Universal Time or Greenwich Civil Time

| Day of Month & Week | The Sun's Apparent Declination | Diff in Declin for 1 hour | Equation of Time | | | GHA of Polaris |
|---------------------|--------------------------------|---------------------------|-------------------------|-------------------|----------------|----------------|
| | | | True Sol. Time = (L.T.) | Differ for 1 hour | GHA of Polaris | |
| 1 TH | S14 25.1 | 0.80 | +16 23.9 | 0.05 | 0 16 | 10.5 |
| 2 FR | S14 44.2 | 0.79 | +16 25.2 | 0.02 | 0 17 | 09.7 |
| 3 SA | S15 03.1 | 0.78 | +16 25.7 | 0.01 | 0 18 | 08.9 |
| 4 SU | S15 21.7 | 0.77 | +16 25.4 | 0.05 | 0 19 | 08.0 |
| 5 M | S15 40.1 | 0.75 | +16 24.3 | 0.08 | 0 0 | 07.2 |
| 6 TU | S15 58.2 | 0.74 | +16 22.3 | 0.12 | 0 1 | 06.3 |
| 7 W | S16 16.1 | 0.73 | +16 19.5 | 0.15 | 0 2 | 05.5 |
| 8 TH | S16 33.6 | 0.72 | +16 15.9 | 0.19 | 0 3 | 04.6 |
| 9 FR | S16 50.9 | 0.71 | +16 11.5 | 0.22 | 0 4 | 03.7 |
| 10 SA | S17 07.9 | 0.70 | +16 06.2 | 0.26 | 0 5 | 02.9 |
| 11 SU | S17 24.7 | 0.68 | +16 00.1 | 0.29 | 0 6 | 02.0 |
| 12 M | S17 41.1 | 0.67 | +15 53.1 | 0.33 | 0 7 | 01.1 |
| 13 TU | S17 57.2 | 0.66 | +15 45.2 | 0.36 | 0 8 | 00.2 |
| 14 W | S18 13.0 | 0.65 | +15 36.5 | 0.40 | 0 8 | 59.4 |
| 15 TH | S18 28.5 | 0.63 | +15 26.9 | 0.44 | 0 9 | 58.6 |
| 16 FR | S18 43.7 | 0.62 | +15 16.4 | 0.47 | 0 0 | 57.9 |
| 17 SA | S18 58.5 | 0.60 | +15 05.1 | 0.51 | 0 1 | 57.1 |
| 18 SU | S19 13.0 | 0.59 | +14 52.9 | 0.54 | 0 2 | 56.4 |
| 19 M | S19 27.1 | 0.58 | +14 39.9 | 0.58 | 0 3 | 55.7 |
| 20 TU | S19 40.9 | 0.56 | +14 26.1 | 0.61 | 0 4 | 54.9 |
| 21 W | S19 54.4 | 0.55 | +14 11.4 | 0.65 | 0 5 | 54.1 |
| 22 TH | S20 07.5 | 0.53 | +13 55.9 | 0.68 | 0 6 | 53.3 |
| 23 FR | S20 20.2 | 0.51 | +13 39.6 | 0.71 | 0 7 | 52.5 |
| 24 SA | S20 32.5 | 0.50 | +13 22.5 | 0.74 | 0 8 | 51.7 |
| 25 SU | S20 44.5 | 0.48 | +13 04.6 | 0.78 | 0 9 | 50.9 |
| 26 M | S20 56.1 | 0.47 | +12 46.0 | 0.81 | 0 0 | 50.1 |
| 27 TU | S21 07.3 | 0.45 | +12 26.7 | 0.83 | 0 1 | 49.4 |
| 28 W | S21 18.0 | 0.43 | +12 06.6 | 0.86 | 0 2 | 48.7 |
| 29 TH | S21 28.4 | 0.42 | +11 45.9 | 0.89 | 0 3 | 48.0 |
| 30 FR | S21 38.4 | 0.40 | +11 24.5 | 0.92 | 0 4 | 47.4 |
| 31 SA | S21 47.9 | | +11 02.5 | | 0 5 | 46.7 |

Hourly differences in declination and equation of time are for the 24 hours following 0-hours of date in left column.

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TABLE 2a

To correct Table 2. See Exam. for below.
MULTIPLIERS FOR OBSERVED BAROMETRIC PRESSURE OR ELEVATION

| Bar. (Inches) | Elev. (Feet) | Multi-plier | Bar. (Inches) | Elev. (Feet) | Multi-plier |
|---------------|--------------|-------------|---------------|--------------|-------------|
| 30.5 | - 451 | 1.03 | 23.9 | 6194 | 0.81 |
| 30.2 | - 181 | 1.02 | 23.6 | 6538 | 0.80 |
| 30.0 | 00 | 1.01 | 23.3 | 6887 | 0.79 |
| 29.8 | 91 | 1.01 | 23.0 | 7239 | 0.78 |
| 29.6 | 186 | 1.00 | 22.7 | 7597 | 0.77 |
| 29.3 | 443 | 0.99 | 22.4 | 7960 | 0.76 |
| 29.0 | 694 | 0.98 | 22.1 | 8327 | 0.75 |
| 28.7 | 1207 | 0.97 | 21.8 | 8700 | 0.74 |
| 28.4 | 1493 | 0.96 | 21.5 | 9077 | 0.73 |
| 28.1 | 1783 | 0.95 | 21.2 | 9460 | 0.72 |
| 27.8 | 2075 | 0.94 | 20.9 | 9848 | 0.71 |
| 27.5 | 2371 | 0.93 | 20.6 | 10242 | 0.70 |
| 27.2 | 2670 | 0.92 | 20.3 | 10642 | 0.69 |
| 26.9 | 2972 | 0.91 | 20.0 | 11047 | 0.68 |
| 26.6 | 3277 | 0.90 | 19.7 | 11458 | 0.67 |
| 26.3 | 3586 | 0.89 | 19.4 | 11875 | 0.66 |
| 26.0 | 3899 | 0.88 | 19.1 | 12299 | 0.65 |
| 25.7 | 4215 | 0.87 | 18.8 | 12729 | 0.64 |
| 25.4 | 4536 | 0.86 | 18.5 | 13165 | 0.63 |
| 26.1 | 4859 | 0.85 | 18.2 | 13608 | 0.62 |
| 24.8 | 5186 | 0.84 | 17.9 | 14058 | 0.61 |
| 24.5 | 5518 | 0.83 | | | |
| 24.2 | 5854 | 0.82 | | | |

MULTIPLIERS FOR TEMPERATURE

| Temp. Deg. F | Multi-plier | Temp. Deg. F | Multi-plier | Temp. Deg. F | Multi-plier |
|--------------|-------------|--------------|-------------|--------------|-------------|
| 20 | 1.16 | 1 30 | 1.04 | 1 80 | 0.94 |
| 10 | 1.13 | 1 40 | 1.02 | 1 90 | 0.93 |
| 0 | 1.11 | 1 50 | 1.00 | 1 100 | 0.91 |
| 1 10 | 1.08 | 1 60 | 0.98 | 1 110 | 0.90 |
| 1 20 | 1.06 | 1 70 | 0.96 | 1 120 | 0.88 |

Example. Sun: Meas. Alt. = 30°; Bar. = 2 in. or Elev. 3900 ft.; Temp. 70° F.
Refraction = 1.66' (0.88) (0.96) = 1.40'. Parallax = 0.13'.
True Alt. = 30° 00.00' - 1.40' + 0.13' = 28° 58.73'.

Example. Star: Meas. Alt. = 25°; Bar. = 24.5 in. or Elev. 5518 ft.; Temp. 10° F.
Refraction = 2.05' (0.83) (1.00) = 1.84'.
True Alt. = 25° 00.00' - 1.84' = 23° 58.16'.