



PRINCE OF SULTAN UNIVERSITY
FACULTY OF ENGINEERING
Department of Computer Engineering

Final Examination: Semester 1

Academic Year: 2007-2008

Date: Wednesday, 3rd October, 2007

Time: 13:30 – 16:30 (**3 hours**)

Subject Number: 240-304

Room: R200

Subject Title: Mathematics for Computer Engineering

Lecturer: Aj. Andrew Davison

Exam Duration: 3 hours

This paper has 4 pages.

Authorized Materials:

- Writing instruments (e.g. pens, pencils).
- Books (e.g. dictionaries) and calculators are **not** permitted.

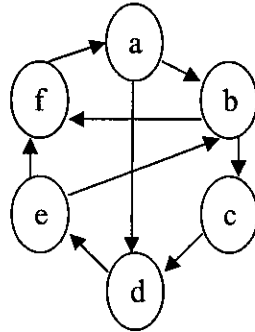
Instructions to Students:

- *Answer questions in English.* Perfect English is **not** required.
- Attempt all questions.
- Write your answers in an answer book.
- Start your answer to each question on a new page
- Clearly number your answers.
- Any unreadable parts will be considered wrong.
- When writing programs, use good layout, and short comments; marks will not be deducted for minor syntax errors.
- The marks for each part of a question are given in brackets (...).

Question 1

(30 marks; 30 minutes)

For the following graph:



- Draw an adjacency list for the graph. (10)
- Draw an adjacency matrix for the graph. (5)
- Give the ANSI C data types for the adjacency list **and** the adjacency matrix. (10)
- If the adjacency matrix is called A , what does an entry in row i and column j mean in A^3 ? (5)

Question 2

(30 marks; 30 minutes)

For the table below:

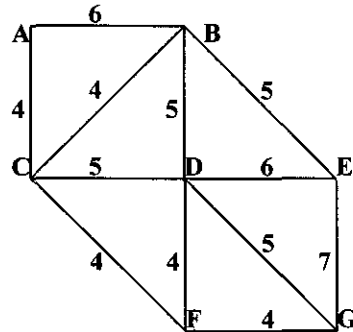
- Draw a graph. The cities should be nodes, the distances edges. (10)
- Using Dijkstra's algorithm, find the shortest distances from Detroit to **all** the other cities. If a city cannot be reached from Detroit, then its minimum distance should be "infinity". Show **all** your working. (20)

| City 1 | City 2 | Distance |
|--------------|------------------|----------|
| Marquette | Sault Ste. Marie | 153 |
| Saginaw | Flint | 31 |
| Grand Rapids | Lansing | 60 |
| Detroit | Lansing | 78 |
| Escanba | Sault Ste. Marie | 175 |
| Ann Arbor | Detroit | 28 |
| Ann Arbor | Battle Creek | 89 |
| Battle Creek | Kalamazoo | 21 |
| Menominee | Escanba | 56 |
| Kalamazoo | Grand Rapids | 45 |
| Escanba | Marquette | 78 |
| Battle Creek | Lansing | 40 |
| Flint | Detroit | 58 |

Question 3

(30 marks; 30 minutes)

Consider the following graph:



- Use Prim's algorithm to find the minimum spanning tree. Show your working. (15)
- Use Kruskal's algorithm to find the minimum spanning tree. Show your working. (15)

Question 4

(30 marks; 30 minutes)

Explain in words the following concepts:

- game tree; (5)
- evaluation function; (5)
- the minimax algorithm; (10)
- alpha-beta pruning. (10)

Each idea should be illustrated with a **brief** example game, such as tic-tac-toe, or another simple game that you know.

Question 5

(30 marks; 30 minutes)

Consider the regular expression:

$$(0 | 1 | 1^*)^*$$

- Draw an automaton with ϵ -transitions for the regular expression. (15)
- Draw an equivalent automaton to the one in (a) *without* using ϵ -transitions. (10)
- Is the automaton of (b) deterministic? If it is not deterministic, draw an equivalent automaton which is deterministic. (5)

Question 6 on next page.

Question 6

(30 marks; 30 minutes)

Consider the following grammar for numbers:

$$\begin{aligned}\text{Number} &\rightarrow \text{Digit Number} \mid \varepsilon \\ \text{Digit} &\rightarrow 0 \mid 1 \mid 2 \mid \dots \mid 9\end{aligned}$$

- Translate the grammar into syntax graphs. (5)
- Translate the syntax graphs into a parser. The parser should print "yes" if the input string matches the grammar; "no" otherwise. The parser should **not** build a parse tree. (15)
- What problems will occur with translating the following grammar rule into a parser function: (5)
$$\text{Number1} \rightarrow \text{Number1 Digit} \mid \text{Digit}$$
- Explain how to translate the grammar rule in (c) into a more suitable form for parsing. Do **not** write syntax graphs or a parser, only the modified grammar. (5)

--- *End of Examination* ---