

PRINCE OF SONGKLA UNIVERSITY
FACULTY OF ENGINEERING

Final Examination: Semester II

Academic Year: 2008

Date: 22 February 2009

Time: 13.30 - 16.30

Subject: 230 - 432 Chemical Engineering Plant

Room: R200

Design

Student Name: Code:

Number of questions : 4 (Total 19 pages)

Time : 3 hours

Total marks : 100

Books and notes are not allowed

Calculators and writing in pencil are allowed.

Data sheets and interest tables are provided at the end of this examination paper.

| Question | Full Marks | Marks Received |
|--------------|------------|----------------|
| 1 | 30 | |
| 2 | 30 | |
| 3 | 20 | |
| 4 | 20 | |
| Total | 100 | |

ทุจริตในการสอบโทษขั้นต่ำคือ ปรับตกในรายวิชาที่ทุจริต และพักการเรียน 1 ภาคการศึกษา

Student Name: Code :

1. a) The purchased-equipment cost of a process plant handling both solids and fluids was estimated to be \$100,000. The plant has high degree of automatic controls and is essentially outdoor operation. A large amount of direct supervision is required. Use the ranges of process-plant component cost outlined in the table below to estimate the fixed-capital cost for the plant. Do not include the land cost in the estimate. Comment on the accuracy of the estimate.

(10 marks)

| Component | Range of Fixed-capital Investment, % |
|--|--------------------------------------|
| Direct costs | |
| Purchased equipment | 15-40 |
| Purchased-equipment installation | 6-14 |
| Instrumentation and controls (installed) | 2-12 |
| Piping (installed) | 4-17 |
| Electrical system (installed) | 2-10 |
| Buildings (including services) | 2-18 |
| Yard improvements | 2-5 |
| Service facilities (installed) | 8-30 |
| Land | 1-2 |
| Indirect costs | |
| Engineering and supervision | 4-20 |
| Construction expenses | 4-17 |
| Legal expenses | 1-3 |
| Contractor's fee | 2-6 |
| Contingency | 5-15 |

Student Name: Code :

- b) Describe the turnover ratio method and its accuracy as the method used for estimating capital investment for a process plant.

(5 marks)

- c) Estimating the manufacturing cost per 100 kg of product under the following conditions:

Fixed-capital investment = \$4 million.

Annual production output = 9 million kg of product.

Raw material costs = \$0.25 /kg of product

Utilities:

1000 kPa steam = 50 kg/kg of product

Purchased electric power = 0.9 kWh/kg of product.

Process water = 0.083 m³/kg of product.

Operating labour = 12 persons per shift, 8 hours/shift, at \$25.00 per employee hour.

Plant operates three hundred 24-h days per year.

Operating supervision is 15 percent of operating labour.

Maintenance and repairs is 0.7 percent of fixed-capital investment.

Operating supplies is 15 percent of maintenance and repairs.

Laboratory charges is 15 percent of operating labour.

There are no patent, royalty, interest, or rent charges.

Plant overhead costs amount to 50 percent of the cost for operating labour, supervision, and maintenance.

Costs for utilities are provided in data sheet at the end of this examination paper.

(15 marks)

Student Name: Code :

2. a) A power plant for generating electricity is part of a plant design proposal. Two alternative power plants with the necessary capacity have been suggested. One uses a boiler and steam turbine while the other uses a gas turbine. The following information applies to the two proposals.

| Power plant type | Boiler and Steam Turbine | Gas Turbine |
|--|-----------------------------|-------------|
| Initial investment, \$ | 600,000 | 400,000 |
| Fuel costs per year, \$ | 160,000 | 230,000 |
| Maintenance and repair per year, \$ | 12,000 | 15,000 |
| Insurance and taxes per year, \$ | 18,000 | 12,000 |
| Service life, yr | 20 | 10 |
| Salvage value at end of service life, \$ | 0 | 0 |

All other costs are the same for either type of power plant. A 12 percent return is required on any investment. If one of these power plants must be accepted, which one should be recommended?

Students may use any methods they prefer for the calculation. For capitalized cost method, the following equations may be useful.

$$K = C_V + \frac{C_R}{(1 + i)^n - 1}$$

- where K = capitalized cost
 C_V = original cost of equipment
 C_R = replacement cost = C_V - salvage value
n = year
i = interest rate

(15 marks)

Student Name: Code :

- b) A new process plant project is estimated to require the fixed capital investment of \$150 million. The salvage value of the plant is \$10 million at the end of plant life of seven year. Estimate the yearly depreciation allowances for seven years using the double declining balance method.

(10 marks)

- c) Acrylic acid is produced by reacting propylene with oxygen. Propylene and air are fed to the reactor at flow rates 127 and 1,363 kmol/h, respectively and must be heated to 190^oC. The reaction is exothermic and yields acrylic acid product and acetic acid by-product at 310^oC. What are the safety considerations that must be paid in designing the reactor?

(5 marks)

Student Name: Code :

3. A rubber products plant is to be built for two years. The fixed-capital costs for the plant is \$40 millions distributed according to percent of construction. A working capital investment of \$ 7.5 millions is needed just before startup. The investing company has its own money and does not need to borrow from a bank.

The project schedule, revenues and operating expenses in millions of dollars are as follows.

| End of year | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|---|----|----|-----|------|------|------|------|------|------|
| % construction | 40 | 60 | | | | | | | |
| Annual revenue | - | - | 7.2 | 12.0 | 18.0 | 24.0 | 28.0 | 30.0 | 32.0 |
| Annual operating Expenses (excluding depreciation) | - | - | 3.8 | 5.3 | 6.5 | 7.4 | 8.2 | 9.1 | 9.8 |

Use the MACRS depreciation schedule with a class life of 5 years (6-year time span) as follows: 20.00%, 32.00%, 19.20%, 11.52%, 11.52% and 5.76%. The income tax rate is 28%.

Write after-tax cash flow for 7-year production.

Calculate the NPV of the project at 10% interest rate.

Calculate the %IRR of the project.

Interest tables are provided at the end of this examination paper.

(20 marks)

Student Name: Code :

4. a) A carbon steel sieve-tray distillation column with 40 trays operated at an average pressure of 303.0 kPa, and average temperature of 147°C is used to separate toluene-benzene feed mixture. The top product contains 99 mole percent of benzene. Tray spacing for the column is 0.61 m. Physical properties at top of the column are:

vapour density, $\rho_v = 6.0 \text{ kg/m}^3$

liquid density, $\rho_L = 830.0 \text{ kg/m}^3$

vapour flow rate, $V = 0.08 \text{ kmol/s}$

liquid flow rate, $L = 0.05 \text{ kmol/s}$

Molecular weight for vapor mixture = 78.00

Surface tension of liquid mixture = 13.27 dynes/cm

Foaming factor = 0.9 and $A_h/A_a > 0.1$

Calculate column diameter at top of column.

(15 marks)

Note:

$L/V = R/(R+1)$, $V=D(R+1)$, R = reflux ratio, D= distillate rate, kmol/s

flooding velocity $V_{nf} = C \left(\frac{\rho_L - \rho_v}{\rho_v} \right)^{1/2}$ ---- (1)

where V_{nf} = net vapour (gas) velocity at flooding, m/s

C = capacity parameter of Souders and Brown

Fair gave a plot of C_{sb} , in the form $C_{sb} = f(\text{tray spacing, } F_{LV})$

where $F_{LV} = \left(\frac{L}{V} \right) \left(\frac{\rho_v}{\rho_L} \right)^{0.5}$, both L and V are in kmol/s

F_{LV} is called "kinetic energy ratio"

C_{sb} is Souders and Brown factor

Student Name: Code :

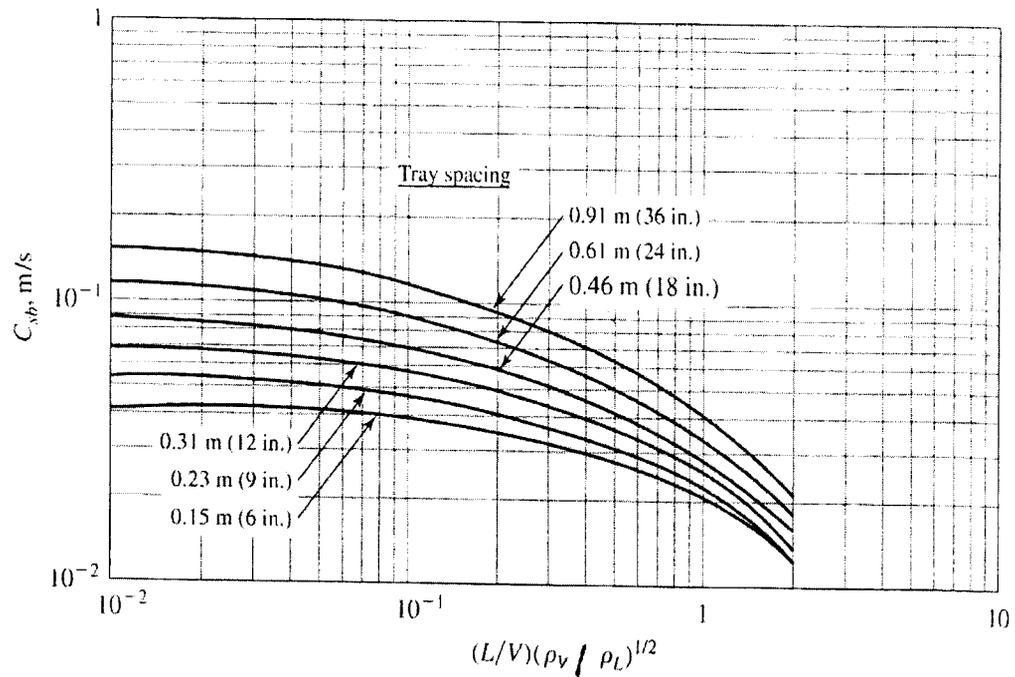


Figure
 Chart for estimating values of C_{sb} (± 10 percent) in Eq. (15-7). [Adapted from *J. R. Fair, Petro/Chem. Eng., 33(10): 45 (1961) with permission.*]

value of C in equation (1) can be calculated from C_{sb}

$$C = F_{ST} F_F F_{HA} C_{sb} \quad \text{----- (2)}$$

- โดย F_{ST} = surface tension factor = $(\sigma/20)^{0.2}$
 F_F = foaming factor (= 1.0 for nonfoaming systems)
 F_{HA} = hole area factor = 1.0 for $A_h/A_a > 0.10$
 A_h = vapour hole area, m^2
 C_{sb} = Souders and Brown factor at flood conditions, m/s
 σ = liquid surface tension, dynes/cm

from the value of C_{sb} obtained from the plot, it is used to find C from equation (2)

and then find V_{nf} from equation (1)

Student Name: Code :

Column diameter can be calculated from

$$\text{column diameter, } D = \left[\frac{4VM_v}{0.85 V_{nf} \pi \left(1 - \frac{A_d}{A}\right) \rho_v} \right]^{0.5} \quad \text{---- (3)}$$

where M_v = molecular weight of vapor

and A = total column cross-sectional area

$$A = \frac{\pi D^2}{4} \quad \text{or} \quad D = (4A/\pi)^{0.5}$$

A_d = area of one downcomer

Oliver suggested that A_d/A can be estimated from the value of F_{LV} as follows

$$A_d/A = 0.1 \quad \text{when } F_{LV} \leq 0.1$$

$$A_d/A = 0.1 + \frac{(F_{LV} - 0.1)}{9} \quad \text{when } 0.1 \leq F_{LV} \leq 1.0$$

$$A_d/A = 0.2 \quad \text{when } F_{LV} \geq 1.0$$

- 4 b) Explain the major items on a balance sheet of a chemical company. Explain the meaning of acid ratio.

(5 marks)

----- End of Examination Questions

Data Sheet

Table **Cost tabulation for selected utilities and labor**

| Utility | Cost |
|---|-------------------|
| Electricity | 0.045 \$/kWh |
| Fuel | |
| Coal | 0.35 \$/GJ |
| Petroleum | 1.30 \$/GJ |
| Petroleum coke | 0.17 \$/GJ |
| Gas | 1.26 \$/GJ |
| Refrigeration, to temperature | |
| 5°C | 20.0 \$/GJ |
| -20°C | 32.0 \$/GJ |
| -50°C | 60.0 \$/GJ |
| Steam, saturated | |
| 10 ³ -10 ⁴ kPa (150-1500 psi) | 4.40 \$/1000 kg |
| Wastewater | |
| Disposal | 0.53 \$/1000 kg |
| Treatment | 0.53 \$/1000 kg |
| Waste | |
| Hazardous | 145.00 \$/1000 kg |
| Nonhazardous | 36.00 \$/1000 kg |
| Water | |
| Cooling | 0.08 \$/1000 kg |
| Process | 0.53 \$/1000 kg |
| Labor | |
| Skilled | 33.67 \$/h |
| Common | 25.00 \$/h |

10% Interest Rate Factors

| N | Single Payment | | | | Equal-Payment Series | | | | Uniform Gradient Series | | | | | | |
|-----|-------------------------------------|-----------------------------------|-------------------------------------|----------------------------------|-----------------------------------|--------------------------------------|----------------------------------|---|-------------------------------------|-----------------------------------|-------------------------------------|----------------------------------|-----------------------------------|--------------------------------------|---|
| | Compound Amount Factor, (P/F, i, N) | Present Worth Factor, (P/F, i, N) | Compound Amount Factor, (F/P, i, N) | Sinking-Fund Factor, (A/F, i, N) | Present Worth Factor, (P/A, i, N) | Capital Recovery Factor, (A/P, i, N) | Sinking-Fund Factor, (A/G, i, N) | Uniform Gradient Series Factor, (A/G, i, N) | Compound Amount Factor, (F/P, i, N) | Present Worth Factor, (P/F, i, N) | Compound Amount Factor, (F/P, i, N) | Sinking-Fund Factor, (A/F, i, N) | Present Worth Factor, (P/A, i, N) | Capital Recovery Factor, (A/P, i, N) | Uniform Gradient Series Factor, (A/G, i, N) |
| | | | | | | | | | | | | | | | |
| 1 | 1.10000 | 0.90909 | 1.00000 | 1.00000 | 0.90909 | 1.10000 | 0.00000 | 0.00000 | 1.12000 | 0.89285 | 1.00000 | 1.00000 | 0.89285 | 1.12000 | 0.00000 |
| 2 | 1.21000 | 0.82644 | 2.10000 | 0.47619 | 1.73553 | 0.57619 | 0.47619 | 0.47619 | 1.25440 | 0.79193 | 1.20000 | 0.47619 | 1.69005 | 0.59169 | 0.47619 |
| 3 | 1.33100 | 0.75131 | 3.31000 | 0.30211 | 2.46852 | 0.40211 | 0.30211 | 0.30211 | 1.40493 | 0.71780 | 1.40000 | 0.29634 | 2.40183 | 0.41639 | 0.30211 |
| 4 | 1.46410 | 0.68301 | 4.64100 | 0.21547 | 3.16965 | 0.31547 | 0.21547 | 0.21547 | 1.57352 | 0.65518 | 1.57000 | 0.20923 | 3.03749 | 0.32923 | 0.21547 |
| 5 | 1.61051 | 0.62092 | 6.10510 | 0.16379 | 3.79076 | 0.26379 | 0.16379 | 0.16379 | 1.75734 | 0.60463 | 1.75000 | 0.15740 | 3.60470 | 0.27409 | 0.16379 |
| 6 | 1.77156 | 0.56473 | 7.71561 | 0.12960 | 4.35267 | 0.22960 | 0.12960 | 0.12960 | 1.93881 | 0.56349 | 1.93000 | 0.11740 | 4.11147 | 0.24325 | 0.12960 |
| 7 | 1.94872 | 0.51358 | 9.48717 | 0.10485 | 4.86948 | 0.18744 | 0.10485 | 0.10485 | 2.12668 | 0.52942 | 2.12000 | 0.09117 | 4.56375 | 0.21917 | 0.10485 |
| 8 | 2.14359 | 0.46650 | 11.43589 | 0.08744 | 5.33926 | 0.15640 | 0.08744 | 0.08744 | 2.32796 | 0.49982 | 2.32000 | 0.07130 | 4.96769 | 0.19789 | 0.08744 |
| 9 | 2.35795 | 0.42409 | 13.57948 | 0.07364 | 5.79023 | 0.13265 | 0.07364 | 0.07364 | 2.54687 | 0.47585 | 2.54000 | 0.05696 | 5.32824 | 0.18167 | 0.07364 |
| 10 | 2.59374 | 0.38543 | 15.93742 | 0.06363 | 6.14567 | 0.11454 | 0.06363 | 0.06363 | 2.78059 | 0.45592 | 2.78000 | 0.04684 | 5.65223 | 0.16984 | 0.06363 |
| 11 | 2.85312 | 0.35049 | 18.53117 | 0.05631 | 6.49061 | 0.10054 | 0.05631 | 0.05631 | 3.03196 | 0.43858 | 3.03000 | 0.03958 | 5.93769 | 0.16154 | 0.05631 |
| 12 | 3.13843 | 0.31863 | 21.38428 | 0.04673 | 6.81361 | 0.08933 | 0.04673 | 0.04673 | 3.29958 | 0.42349 | 3.29000 | 0.03467 | 6.19437 | 0.15652 | 0.04673 |
| 13 | 3.45227 | 0.28966 | 24.52271 | 0.04077 | 7.10356 | 0.08078 | 0.04077 | 0.04077 | 3.58499 | 0.41006 | 3.58000 | 0.03082 | 6.43548 | 0.15367 | 0.04077 |
| 14 | 3.79750 | 0.26333 | 27.97498 | 0.03574 | 7.36687 | 0.07462 | 0.03574 | 0.03574 | 3.88711 | 0.39801 | 3.88000 | 0.02786 | 6.65162 | 0.15168 | 0.03574 |
| 15 | 4.17725 | 0.23932 | 31.77248 | 0.03147 | 7.60679 | 0.07046 | 0.03147 | 0.03147 | 4.20646 | 0.38711 | 4.20000 | 0.02549 | 6.84436 | 0.15023 | 0.03147 |
| 16 | 4.59497 | 0.21762 | 35.94973 | 0.02781 | 7.82378 | 0.06786 | 0.02781 | 0.02781 | 4.54307 | 0.37711 | 4.54000 | 0.02359 | 7.01433 | 0.14923 | 0.02781 |
| 17 | 5.05447 | 0.19784 | 40.54470 | 0.02464 | 8.01812 | 0.06611 | 0.02464 | 0.02464 | 4.89804 | 0.36801 | 4.89000 | 0.02200 | 7.18331 | 0.14856 | 0.02464 |
| 18 | 5.55992 | 0.17985 | 45.59917 | 0.02193 | 8.19421 | 0.06520 | 0.02193 | 0.02193 | 5.27059 | 0.35958 | 5.27000 | 0.02070 | 7.34133 | 0.14811 | 0.02193 |
| 19 | 6.11591 | 0.16350 | 51.15909 | 0.01954 | 8.35367 | 0.06491 | 0.01954 | 0.01954 | 5.66920 | 0.35181 | 5.66000 | 0.01960 | 7.48866 | 0.14784 | 0.01954 |
| 20 | 6.72750 | 0.14864 | 57.27500 | 0.01745 | 8.49836 | 0.06503 | 0.01745 | 0.01745 | 6.08429 | 0.34469 | 6.08000 | 0.01860 | 7.62544 | 0.14762 | 0.01745 |
| 21 | 7.40025 | 0.13513 | 64.00250 | 0.01562 | 8.63080 | 0.06537 | 0.01562 | 0.01562 | 6.51682 | 0.33811 | 6.51000 | 0.01770 | 7.75244 | 0.14750 | 0.01562 |
| 22 | 8.14027 | 0.12286 | 71.40273 | 0.01405 | 8.75143 | 0.06570 | 0.01405 | 0.01405 | 7.00000 | 0.33201 | 7.00000 | 0.01690 | 7.86966 | 0.14744 | 0.01405 |
| 23 | 8.94973 | 0.11167 | 79.54302 | 0.01271 | 8.86084 | 0.06603 | 0.01271 | 0.01271 | 7.45782 | 0.32631 | 7.45000 | 0.01620 | 7.97722 | 0.14741 | 0.01271 |
| 24 | 9.81973 | 0.10126 | 88.34706 | 0.01161 | 8.96045 | 0.06635 | 0.01161 | 0.01161 | 7.92640 | 0.32101 | 7.92000 | 0.01560 | 8.07544 | 0.14739 | 0.01161 |
| 25 | 10.75181 | 0.09159 | 97.81177 | 0.01069 | 9.05190 | 0.06666 | 0.01069 | 0.01069 | 8.40636 | 0.31611 | 8.40000 | 0.01510 | 8.17440 | 0.14737 | 0.01069 |
| 26 | 11.74699 | 0.08355 | 107.91177 | 0.00995 | 9.13625 | 0.06696 | 0.00995 | 0.00995 | 8.89858 | 0.31161 | 8.89000 | 0.01460 | 8.26440 | 0.14735 | 0.00995 |
| 27 | 12.80999 | 0.07677 | 118.64942 | 0.00934 | 9.21425 | 0.06725 | 0.00934 | 0.00934 | 9.40259 | 0.30741 | 9.40000 | 0.01420 | 8.34640 | 0.14733 | 0.00934 |
| 28 | 14.04209 | 0.07109 | 131.03994 | 0.00883 | 9.28733 | 0.06753 | 0.00883 | 0.00883 | 9.92840 | 0.30351 | 9.92000 | 0.01380 | 8.42040 | 0.14731 | 0.00883 |
| 29 | 15.45309 | 0.06639 | 144.83093 | 0.00840 | 9.35605 | 0.06780 | 0.00840 | 0.00840 | 10.47440 | 0.30001 | 10.47000 | 0.01340 | 8.48640 | 0.14729 | 0.00840 |
| 30 | 17.04940 | 0.06250 | 161.14940 | 0.00803 | 9.42098 | 0.06806 | 0.00803 | 0.00803 | 11.14400 | 0.29681 | 11.14000 | 0.01300 | 8.54440 | 0.14727 | 0.00803 |
| 31 | 18.84334 | 0.05920 | 179.94334 | 0.00771 | 9.48262 | 0.06831 | 0.00771 | 0.00771 | 11.93840 | 0.29391 | 11.93000 | 0.01260 | 8.60440 | 0.14725 | 0.00771 |
| 32 | 20.84767 | 0.05641 | 201.13777 | 0.00743 | 9.54065 | 0.06855 | 0.00743 | 0.00743 | 12.85840 | 0.29131 | 12.85000 | 0.01220 | 8.66640 | 0.14723 | 0.00743 |
| 33 | 23.22515 | 0.05406 | 222.25154 | 0.00719 | 9.59558 | 0.06878 | 0.00719 | 0.00719 | 13.90440 | 0.28891 | 13.90000 | 0.01180 | 8.73040 | 0.14721 | 0.00719 |
| 34 | 25.94767 | 0.05208 | 245.47670 | 0.00698 | 9.64805 | 0.06900 | 0.00698 | 0.00698 | 15.08840 | 0.28671 | 15.08000 | 0.01140 | 8.79640 | 0.14719 | 0.00698 |
| 35 | 29.07266 | 0.05034 | 271.02437 | 0.00679 | 9.70765 | 0.06921 | 0.00679 | 0.00679 | 16.41440 | 0.28471 | 16.41000 | 0.01100 | 8.86440 | 0.14717 | 0.00679 |
| 36 | 30.91266 | 0.04881 | 299.12681 | 0.00661 | 9.76392 | 0.06941 | 0.00661 | 0.00661 | 17.88840 | 0.28291 | 17.88000 | 0.01060 | 8.93440 | 0.14715 | 0.00661 |
| 37 | 34.00949 | 0.04734 | 330.03949 | 0.00644 | 9.81745 | 0.06960 | 0.00644 | 0.00644 | 19.51440 | 0.28131 | 19.51000 | 0.01020 | 9.00640 | 0.14713 | 0.00644 |
| 38 | 37.40434 | 0.04599 | 364.04343 | 0.00628 | 9.86874 | 0.06978 | 0.00628 | 0.00628 | 21.30440 | 0.27991 | 21.30000 | 0.01000 | 9.08140 | 0.14711 | 0.00628 |
| 39 | 41.14478 | 0.04474 | 401.44778 | 0.00613 | 9.91834 | 0.06995 | 0.00613 | 0.00613 | 23.25840 | 0.27871 | 23.25000 | 0.00980 | 9.15940 | 0.14709 | 0.00613 |
| 40 | 45.25926 | 0.04358 | 442.59256 | 0.00599 | 9.96665 | 0.07011 | 0.00599 | 0.00599 | 25.39240 | 0.27771 | 25.39000 | 0.00960 | 9.24140 | 0.14707 | 0.00599 |
| 42 | 54.76370 | 0.04260 | 537.63699 | 0.00586 | 10.01373 | 0.07026 | 0.00586 | 0.00586 | 27.72040 | 0.27691 | 27.72000 | 0.00940 | 9.32740 | 0.14705 | 0.00586 |
| 48 | 97.01723 | 0.04105 | 960.17234 | 0.00572 | 10.10415 | 0.07040 | 0.00572 | 0.00572 | 30.36040 | 0.27631 | 30.36000 | 0.00920 | 9.41740 | 0.14703 | 0.00572 |
| 50 | 117.39065 | 0.04053 | 1163.90853 | 0.00567 | 10.14814 | 0.07049 | 0.00567 | 0.00567 | 33.20440 | 0.27591 | 33.20000 | 0.00910 | 9.51140 | 0.14701 | 0.00567 |
| 60 | 304.68164 | 0.04012 | 3034.81640 | 0.00562 | 10.22945 | 0.07057 | 0.00562 | 0.00562 | 36.36840 | 0.27571 | 36.36000 | 0.00900 | 9.61740 | 0.14699 | 0.00562 |
| 70 | 789.74696 | 0.04000 | 7887.66957 | 0.00561 | 10.29949 | 0.07061 | 0.00561 | 0.00561 | 40.86440 | 0.27561 | 40.86000 | 0.00890 | 9.73440 | 0.14697 | 0.00561 |
| 80 | 1271.89537 | 0.04000 | 12708.95371 | 0.00561 | 10.35843 | 0.07063 | 0.00561 | 0.00561 | 45.86440 | 0.27561 | 45.86000 | 0.00880 | 9.86140 | 0.14695 | 0.00561 |
| 90 | 2048.40021 | 0.04000 | 20476.00215 | 0.00561 | 10.40782 | 0.07064 | 0.00561 | 0.00561 | 51.46440 | 0.27561 | 51.46000 | 0.00870 | 9.99940 | 0.14693 | 0.00561 |
| 100 | 33780.61234 | 0.04000 | 33776.12340 | 0.00561 | 10.44814 | 0.07064 | 0.00561 | 0.00561 | 57.76440 | 0.27561 | 57.76000 | 0.00860 | 10.14740 | 0.14691 | 0.00561 |

12% Interest Rate Factors

| N | Single Payment | | | | Equal-Payment Series | | | | Uniform Gradient Series | | | | | | |
|----|-------------------------------------|-----------------------------------|-------------------------------------|----------------------------------|-----------------------------------|--------------------------------------|----------------------------------|---|-------------------------------------|-----------------------------------|-------------------------------------|----------------------------------|-----------------------------------|--------------------------------------|---|
| | Compound Amount Factor, (P/F, i, N) | Present Worth Factor, (P/F, i, N) | Compound Amount Factor, (F/P, i, N) | Sinking-Fund Factor, (A/F, i, N) | Present Worth Factor, (P/A, i, N) | Capital Recovery Factor, (A/P, i, N) | Sinking-Fund Factor, (A/G, i, N) | Uniform Gradient Series Factor, (A/G, i, N) | Compound Amount Factor, (F/P, i, N) | Present Worth Factor, (P/F, i, N) | Compound Amount Factor, (F/P, i, N) | Sinking-Fund Factor, (A/F, i, N) | Present Worth Factor, (P/A, i, N) | Capital Recovery Factor, (A/P, i, N) | Uniform Gradient Series Factor, (A/G, i, N) |
| | | | | | | | | | | | | | | | |
| 1 | 1.12000 | 0.89285 | 1.00000 | 1.00000 | 0.89285 | 1.12000 | 0.00000 | 0.00000 | 1.12000 | 0.89285 | 1.00000 | 1.00000 | 0.89285 | 1.12000 | 0.00000 |
| 2 | 1.25440 | 0.79193 | 1.25440 | 0.47619 | 1.69005 | 0.57619 | 0.47619 | 0.47619 | 1.25440 | 0.79193 | 1.20000 | 0.47619 | 1.69005 | 0.59169 | 0.47619 |
| 3 | 1.40493 | 0.71780 | 1.40493 | 0.30211 | 2.40183 | 0.40211 | 0.30211 | 0.30211 | 1.40493 | 0.71780 | 1.40000 | 0.29634 | 2.40183 | 0.41639 | 0.30211 |
| 4 | 1.57352 | 0.65518 | 1.57352 | 0.21547 | 3.03749 | 0.31547 | 0.21547 | 0.21547 | 1.57352 | 0.65518 | 1.57000 | 0.20923 | 3.03749 | 0.32923 | 0.21547 |
| 5 | 1.75734 | 0.60463 | 1.75734 | 0.16379 | 3.60470 | 0.26379 | 0.16379 | 0.16379 | 1.75734 | 0.60463 | 1.75000 | 0.15740 | 3.60470 | 0.27409 | 0.16379 |
| 6 | 1.93881 | 0.56349 | 1.93881 | 0.12960 | 4.11147 | 0.22960 | 0.12960 | 0.12960 | 1.93881 | 0.56349 | 1.93000 | 0.11740 | 4.11147 | 0.24325 | 0.12960 |
| 7 | 2.12668 | 0.52942 | 2.12668 | 0.10485 | 4.56375 | 0.18744 | 0.10485 | 0.10485 | 2.12668 | 0.52942 | 2.12000 | 0.09117 | 4.56375 | 0.21917 | 0.10485 |
| 8 | 2.32796 | 0.49982 | 2.32796 | 0.08744 | 4.96769 | 0.15640 | 0.08744 | 0.08744 | 2.32796 | 0.49982 | 2.32000 | 0.07130 | 4.96769 | 0.19789 | 0.08744 |
| 9 | 2.54687 | 0.47585 | 2.54687 | 0.07364 | 5.32824 | 0.13265 | 0.07364 | 0.07364 | 2.54687 | 0.47585 | 2.54000 | 0.05696 | 5.32824 | 0.18167 | 0.07364 |
| 10 | 2.78059 | 0.45592 | 2.78059 | 0.06363 | 5.65223 | 0.11454 | 0.06363 | 0.06363 | 2.78059 | 0. | | | | | |