

มหาวิทยาลัยสงขลานครินทร์
คณะวิศวกรรมศาสตร์

การสอบกลางภาค: ประจำภาคการศึกษาที่ 1

วันที่: 30 กรกฎาคม 2552

วิชา: 220-502 Advanced Mechanics of Solids

ปีการศึกษา: 2552

เวลา: 09.00-12.00 น.

ห้อง: R201

คำอธิบาย

1. ข้อสอบมีจำนวนทั้งหมด 5 ข้อ
2. ให้เลือกทำข้อสอบ 4 ข้อ
3. อนุญาตให้นำเครื่องคิดเลขทุกชนิดเข้าห้องสอบได้ และให้นำตำราเรียน, เอกสารทุกชนิด เข้าห้องสอบได้
4. ไม่ต้องส่งกระดาษทดเลขที่แจกให้คืน

ข้อ	คะแนนเต็ม	ได้คะแนน
1	25	
2	35	
3	25	
4	25	
5	25	
รวม		

ผู้ออกข้อสอบ: บุญ จันทร์ทักษิณภาส

1. (25 points) At a point in a member, the stress components are found to be

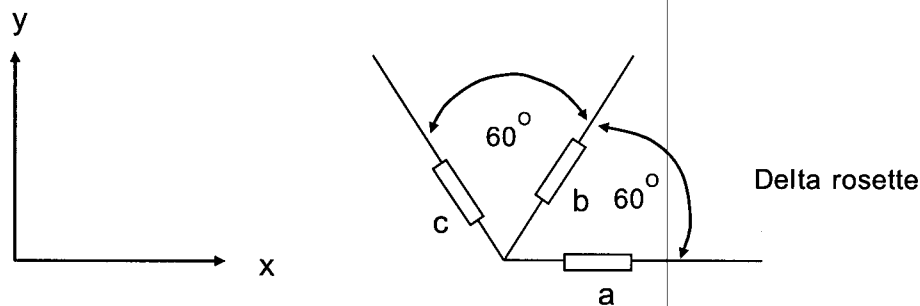
$$\sigma_{xx} = 18.8 \text{ MPa}, \sigma_{yy} = 5.0 \text{ MPa}, \sigma_{zz} = 25.0 \text{ MPa}, \sigma_{xy} = -7.0 \text{ MPa}, \sigma_{xz} = -15.0 \text{ MPa}, \sigma_{yz} = 0.0 \text{ MPa}$$

- (a) Determine magnitudes of the **principal stresses** and the **maximum shear stress**.
- (b) Determine magnitudes of the **normal** and **shear** stress components acting on a plane whose normal lies in the **x-y plane** and making an angle of 60° with the **x-axis**.
- (c) Determine the direction of the **minimum principal stress** (σ_3).

2. (35 points)

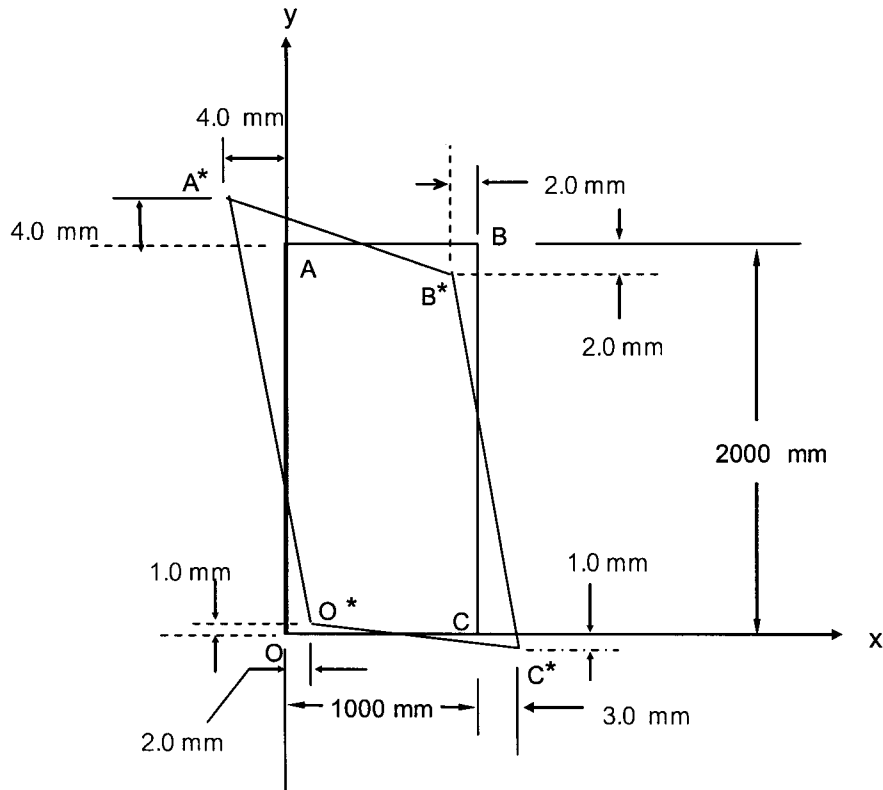
A delta rosette shown below is cemented to a point on the free surface of a **plane stress** member (stressed in the x-y plane). From measurements, $\varepsilon_a = 2.580 \times 10^{-4}$, $\varepsilon_b = 1.250 \times 10^{-4}$, $\varepsilon_c = -1.800 \times 10^{-4}$.

- (a). (10 points) Determine the magnitudes and orientations of the **principal strains** in the x-y plane at that point.
- (b) (15 points) Determine the magnitudes of **stress components** at that point if the member is an **isotropic material** with $\nu = 0.33$, and $E = 720 \text{ GPa}$.
- (c) (10 points) Determine the magnitudes of stress components at that point if the member is an **orthotropic material** with orthotropic axes x, y, z; and with the following material properties, $E_x = 15.00 \text{ GPa}$, $E_y = 12.00 \text{ GPa}$, $E_z = 6.00 \text{ GPa}$, $G_{xy} = 11.00 \text{ GPa}$, $G_{xz} = 10.00 \text{ GPa}$, $G_{yz} = 2.500 \text{ GPa}$, $\nu_{xy} = 0.420$, $\nu_{xz} = 0.400$, $\nu_{yz} = 0.650$

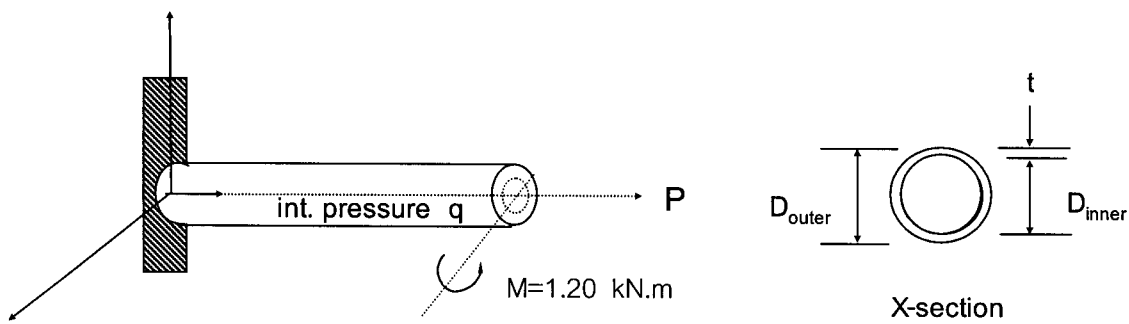


3. (25 points) A rectangular plate **OABC** of dimensions 1000 mm x 2000 mm in the x-y plane shown below is loaded so that the plate is in the state of **plane strain**, ($\varepsilon_{zz} = \varepsilon_{zx} = \varepsilon_{zy} = 0$), and passes to a new position **O*A*B*C***

- (a). Determine the **displacements** (u, v), of the plate for the deformation shown in term of x, y coordinates.
- (b). Determine the **strain components at the point B** of the plate, and evaluate the maximum strain at B.
- (c). Determine the strain at the point B in the direction of the **line BO**.



4. (25 points) A closed-end thin wall steel tube with the yield strength $Y = 320 \text{ MPa}$, has **outside diameter 122 mm and inside diameter 118 mm** (ie. mean diameter of 120 mm and wall thickness of 4 mm). It is subjected to an internal pressure $q = 6 \text{ MPa}$, a bending moment $M = 1.20 \text{ kN.m}$, and an axial external applied load P , as shown below. Using a safety factor $SF = 2.00$, determine the maximum allowable value of the axial load P based on maximum shear stress criterion of failure.



5. (25 points) A solid metal shaft of diameter $d = 120 \text{ mm}$, is subjected to an axial load $P = 220.0 \text{ kN}$, a bending moment $M = 10.00 \text{ kN.m}$, and a torque $T = 15.0 \text{ kN.m}$.

(a) If yield strength for the metal is $Y = 300 \text{ MPa}$, and assuming that failure occurs at the initiation of yielding, determine the factor of safety based on the **octahedral shear stress criterion** of failure.

(b) If the metal is a brittle material with ultimate strength, $\sigma_u = 200 \text{ MPa}$, $E = 200 \text{ GPa}$, $\nu = 0.29$, determine the factor of safety based on the **maximum principal strain criterion** of failure.

