

มหาวิทยาลัยสงขลานครินทร์
คณะวิศวกรรมศาสตร์

การสอบปลายภาคการศึกษา: ประจำปีการศึกษาที่ 1
วันที่: 3 ตุลาคม 2552
วิชา: 220-502 Advanced Mechanics of Solids

ปีการศึกษา: 2552
เวลา: 09.00-12.00 น.
ห้อง: R201

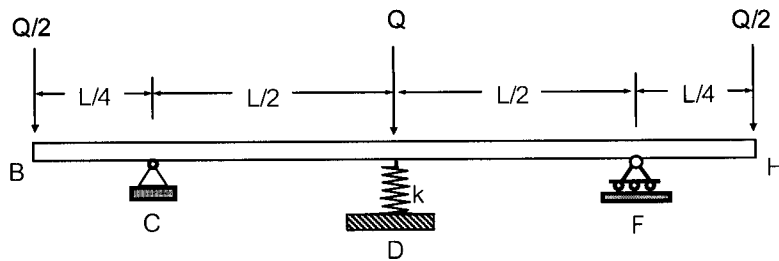
คำอธิบาย

1. ข้อสอบมีจำนวนทั้งหมด 6 ข้อ
2. ให้เลือกทำข้อสอบ 4 ข้อ
3. อนุญาตให้นำเครื่องคิดเลขทุกชนิดเข้าห้องสอบได้ และให้นำตำราเรียน, เอกสารทุกชนิด เข้าห้องสอบได้
4. ไม่ต้องส่งกระดาษทดเลขที่แจกให้คืน

ข้อ	คะแนนเต็ม	ได้คะแนน
1	25	
2	25	
3	25	
4	25	
5	25	
6	25	
รวม		

ผู้ออกข้อสอบ : บุญ จันทร์ทักษิณภาส

1. (25 points) A steel I-beam ($E = 200000 \text{ MPa}$, depth = 200 mm, $I_x = 20.0 \times 10^6 \text{ mm}^4$) is subjected to three applied point loads and supported at C, D, F by a pinned support, a spring support and a roller support respectively, as shown below. Determine the displacement of the beam at mid length and the maximum bending stress in the beam, given $L = 8000 \text{ mm}$, $k = 3.75 \times 10^5 \text{ N/m}$, $Q = 15000 \text{ N}$.



2. (25 points) A hollow thin-wall steel torsion member ($G = 72000 \text{ MPa}$), with cross section shown below in Fig.(a), is subjected to a pure torque T .

(a) If the applied torque $T = 12 \text{ kN.m}$, determine the maximum shear stress developed and calculate the unit angle of twist.

(b) Given that the cross section is an open cross section instead of a closed cross section, Fig.(b), determine the permissible value for T if the maximum shear stress must not be greater than 60 MPa . Evaluate also the corresponding unit angle of twist.

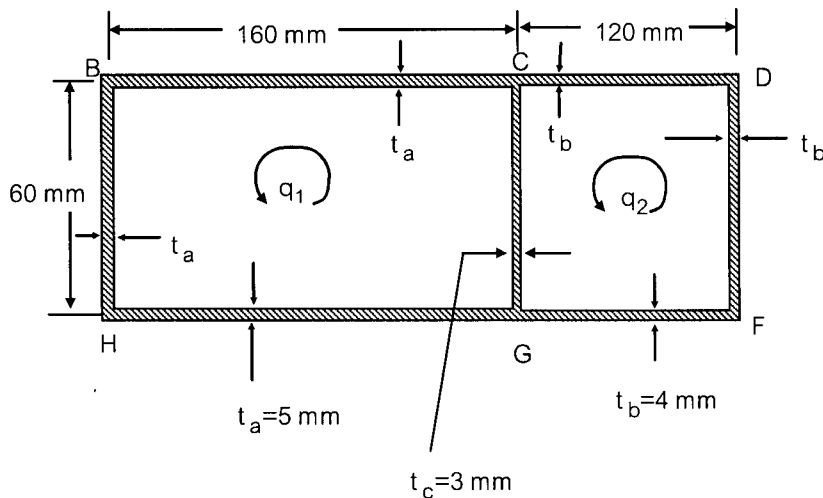


Fig. a

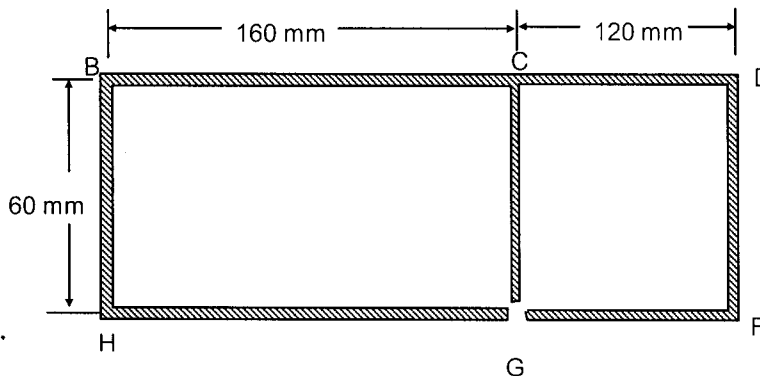


Fig. b

3. (25 points) A steel member ($E = 200000 \text{ MPa}$) with the cross section shown below is used as a cantiliver beam of length $L = 2.0 \text{ m}$. The beam is subjected to a point load $P = 6.0 \text{ kN}$ at the free end passing through the shear centre of the cross-section, and with the direction as shown ($\phi = 60^\circ$).

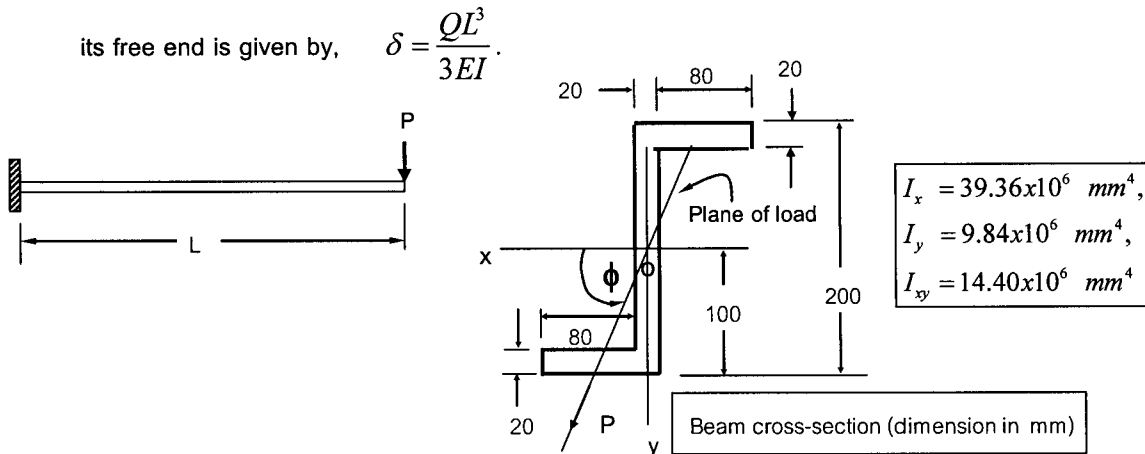
(a) Determine the maximum tensile and compressive stresses in the beam and the deflection at the free end of the beam.

(b) Find a new orientation of the load P such that the beam will have zero horizontal deflection (ie. zero deflection in the x-direction).

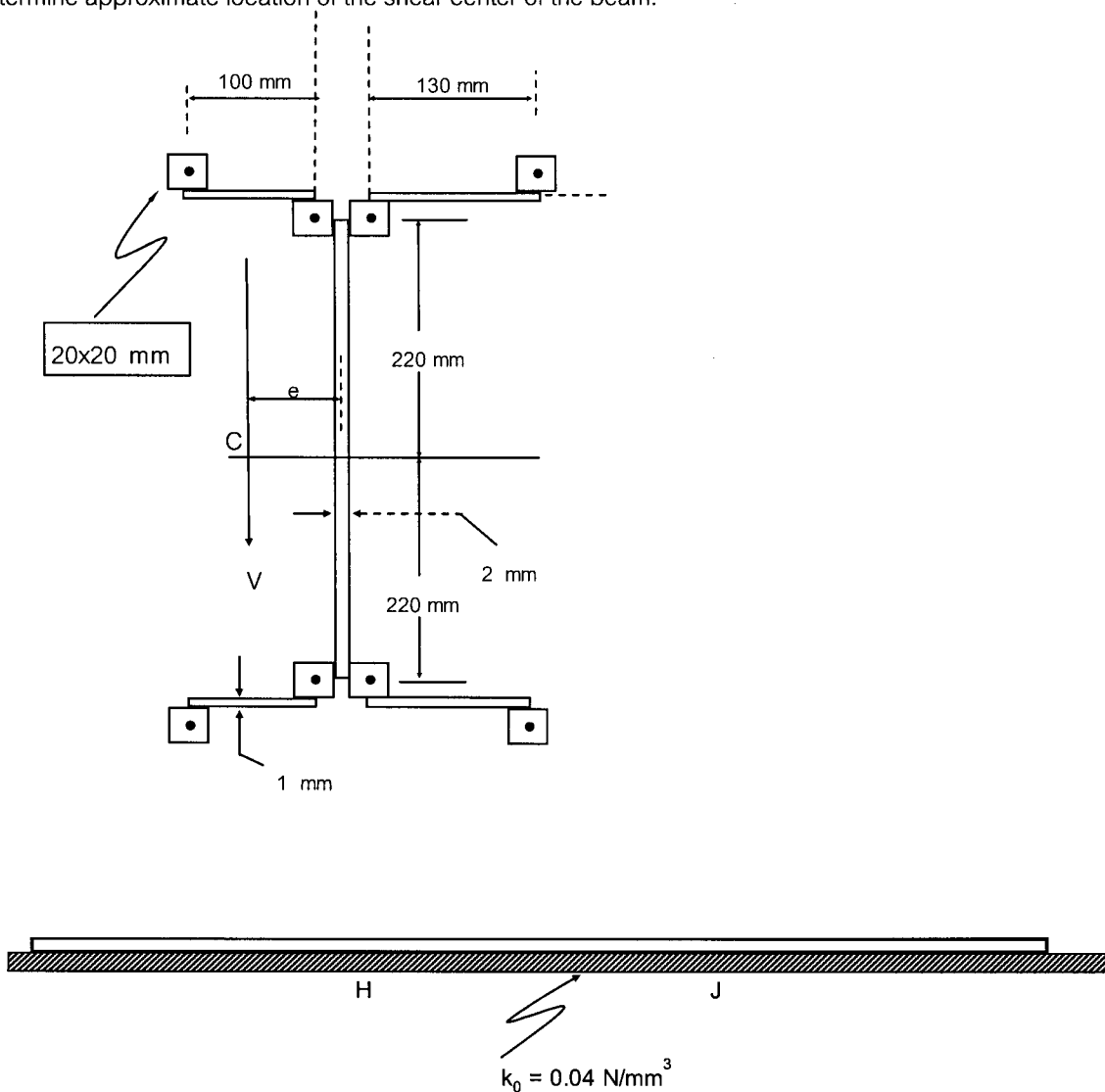
Note : 1. The view shown below is from the free end toward the fixed end of the beam.

2. The deflection at the end of a cantiliver beam of length L symmetrically loaded by a point load, Q , at its free end is given by,

$$\delta = \frac{QL^3}{3EI}$$



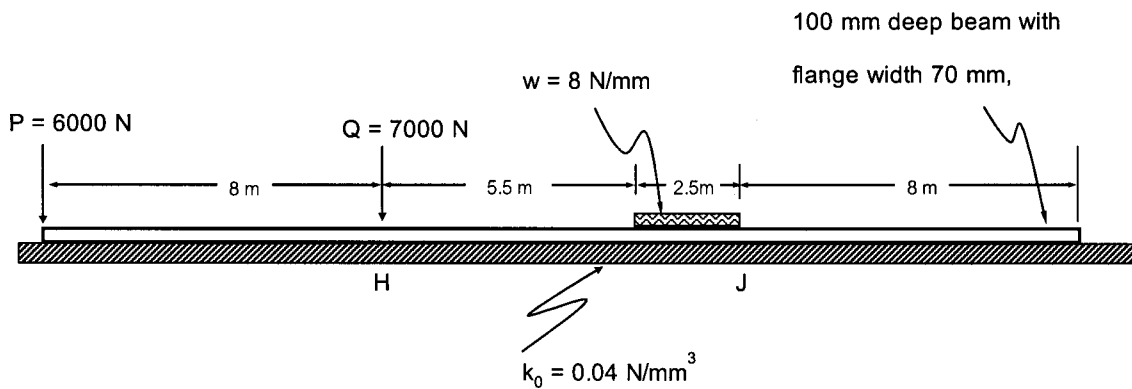
4. (25 points) A composite thin wall beam has symmetrical cross section as shown below. The cross section consists of 2 mm thick vertical web and 1 mm thick flanges welded to 8 square stringers of 20x20 mm cross section. Determine approximate location of the shear center of the beam.



6. (25 points) A closed-end thin wall metal tube has outside diameter 124 mm and inside diameter 116 mm (ie. mean diameter of 120 mm and wall thickness of 4 mm). It is subjected to an internal pressure $q = 4 \text{ MPa}$, a bending moment $M_x = 1.20 \text{ kN.m}$, and an axial external applied load P , as shown below. The material has the following properties. $Y = 320 \text{ MPa}$, $E = 200000 \text{ MPa}$, $\nu = 0.29$

5. (25 points) A steel I-beam ($E = 200000 \text{ GPa}$, depth = 100 mm, flange width $b = 70 \text{ mm}$, $I_x = 2.63 \times 10^6 \text{ mm}^4$) of 24 m in length, is supported on an elastic foundation for which $k_0 = 0.04 \text{ N/mm}^3$. A point load $P = 6000 \text{ N}$, and $Q = 7000 \text{ N}$ and a uniformly distributed load of loaded length 2500 mm and intensity $w = 8 \text{ N/mm}$ is applied to the beam as shown below.

- (a) Determine the maximum deflection of the beam.
- (b) Determine the maximum bending stress in the beam.
- (c) If the point load Q is a moving load which can traverse the middle third of the beam (ie. can move from H to J), determine the maximum deflection and the maximum bending stress in the beam.



6. (25 points) A closed-end thin wall metal tube has outside diameter 124 mm and inside diameter 116 mm (ie. mean diameter of 120 mm and wall thickness of 4 mm). It is subjected to an internal pressure $q = 4 \text{ MPa}$, a bending moment $M_x = 1.20 \text{ kN.m}$, and an axial external applied load P , as shown below. The material has the following properties, $Y = 320 \text{ MPa}$, $E = 200000 \text{ MPa}$, $\nu = 0.29$.

- (a) Determine the maximum allowable value of the axial load P based on the maximum shear stress criterion of failure, using a safety factor $SF = 2.00$.
- (b) If it is found out later that the tube is occasionally subjected to an additional bending moment $M_y = 1.30 \text{ kN.m}$, determine the new value of available safety factor, use the value of external applied load P determined previously in (a).

